

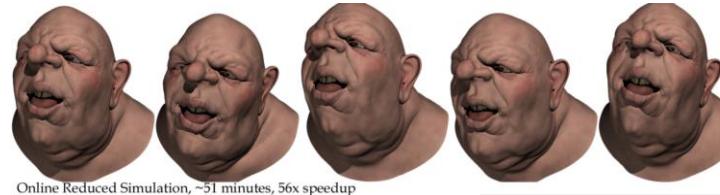
# Deep Fluids: A Generative Network for Parameterized Fluid Simulations

Byungsoo Kim<sup>1</sup> Vinicius C. Azevedo<sup>1</sup> Nils Thuerey<sup>2</sup>  
Theodore Kim<sup>3</sup> Markus Gross<sup>1</sup> Barbara Solenthaler<sup>1</sup>



## » Challenges

- Physically-based **simulations** are still slow
  - Obtaining high-quality results is computationally expensive



Kim & James 2009



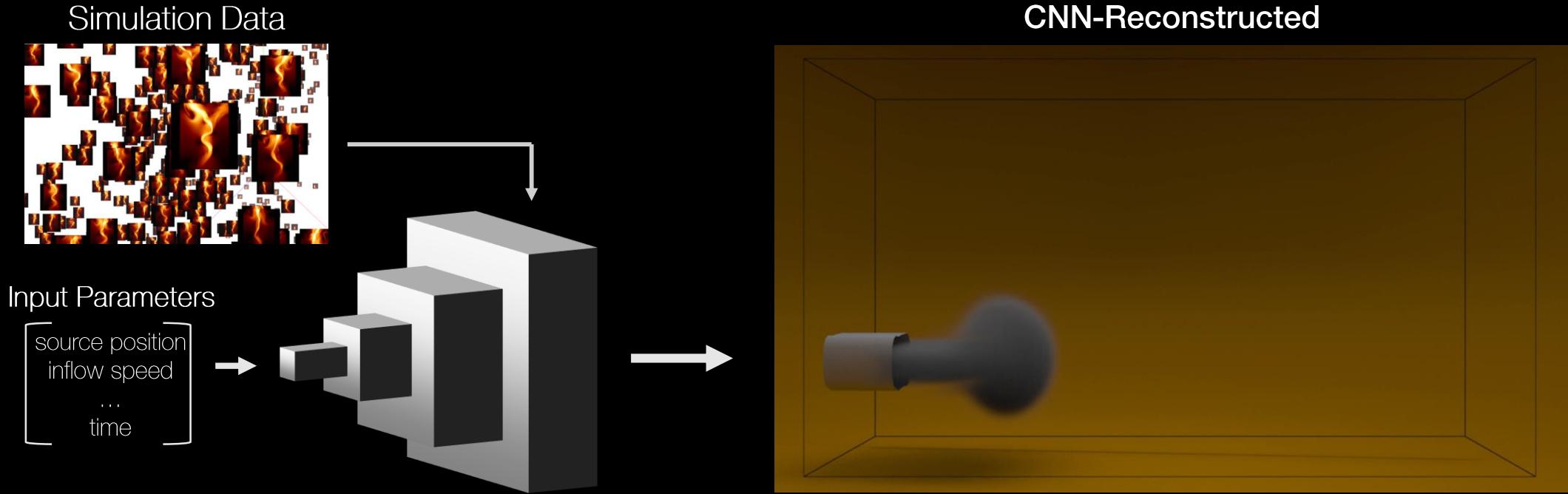
Kim & Delaney 2013



Hahn et al. 2014

- Limited support for artist control
  - Changing an existing **simulation** entails trial & error
- Production data consumes large amount of storage space
  - Growing need to reuse stored simulation data

# Deep-Fluids: A Generative Network for Parameterized Fluid Simulations



## Technical Contributions

- First generative neural network for parametrized Eulerian fluid simulations
- Up to 700x speed-ups compared with underlying CPU solvers for re-simulating the data
- Interpolation between discrete examples across different parameters
- Over 1300x compression ratio for velocity field data
- Novel Latent Space Integrator for complex parameterization

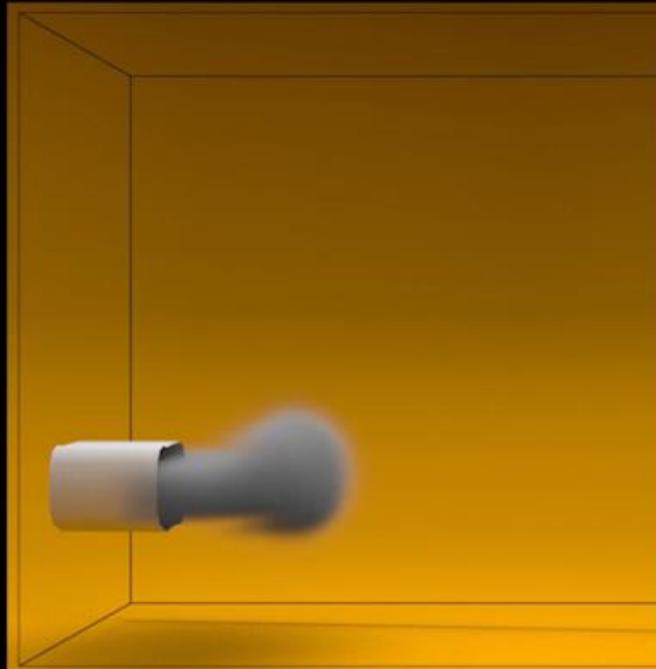


**Ground-Truth** Simulation

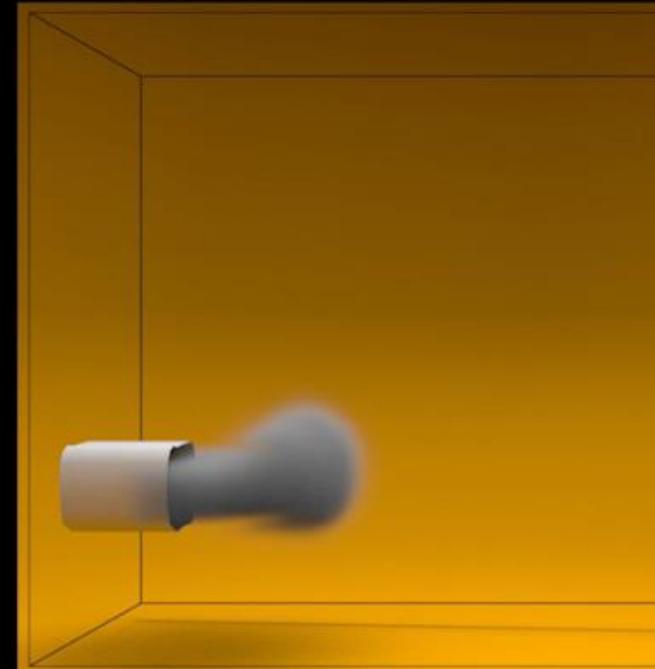


**CNN-Reconstructed** Simulation

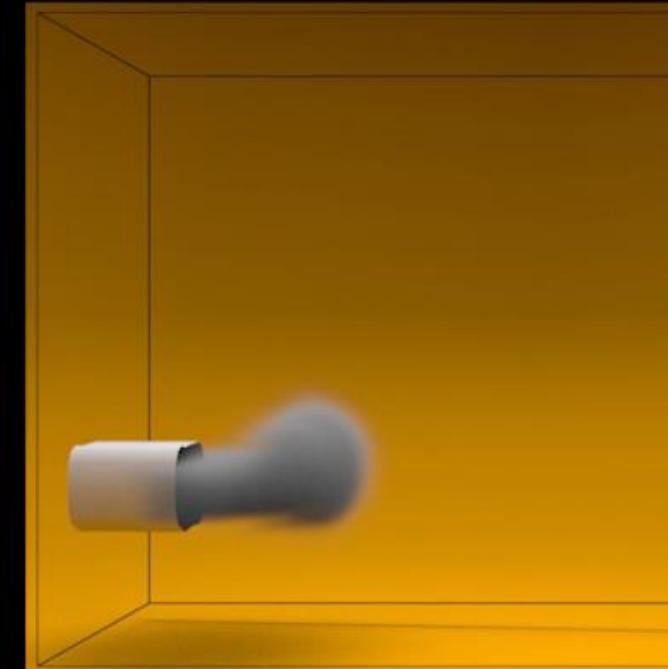
## Buoyancy Interpolation Example



**Direct** correspondence  
for buoyancy  $b = 6 \times 10^{-4}$



**Interpolated** with  $b = 8 \times 10^{-4}$   
**Not present** in the original **data set**



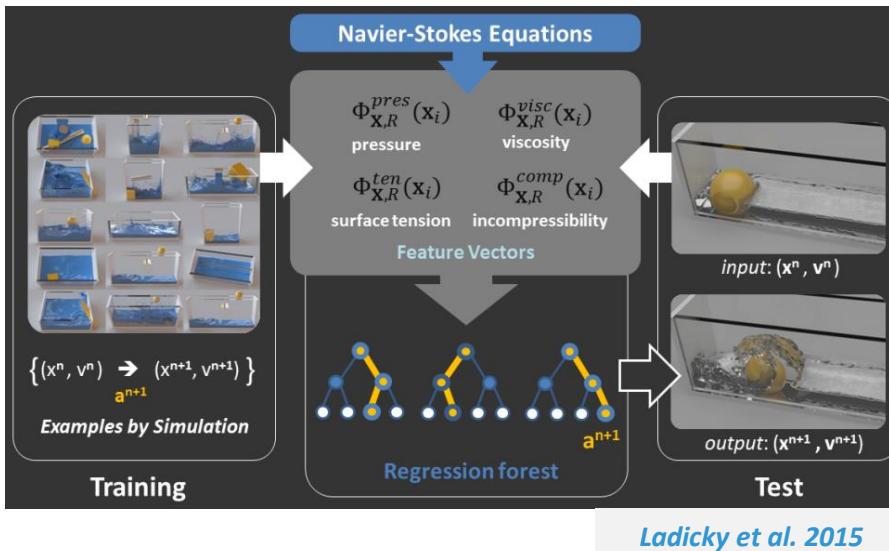
**Direct** correspondence  
for buoyancy  $b = 1 \times 10^{-3}$

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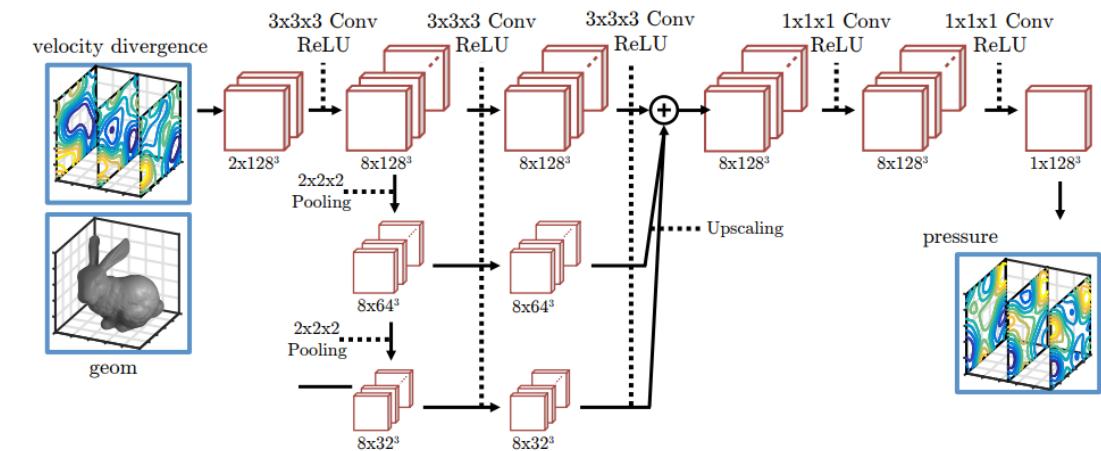
# Machine Learning Research in Fluids

# Machine Learning for Fluid Simulation

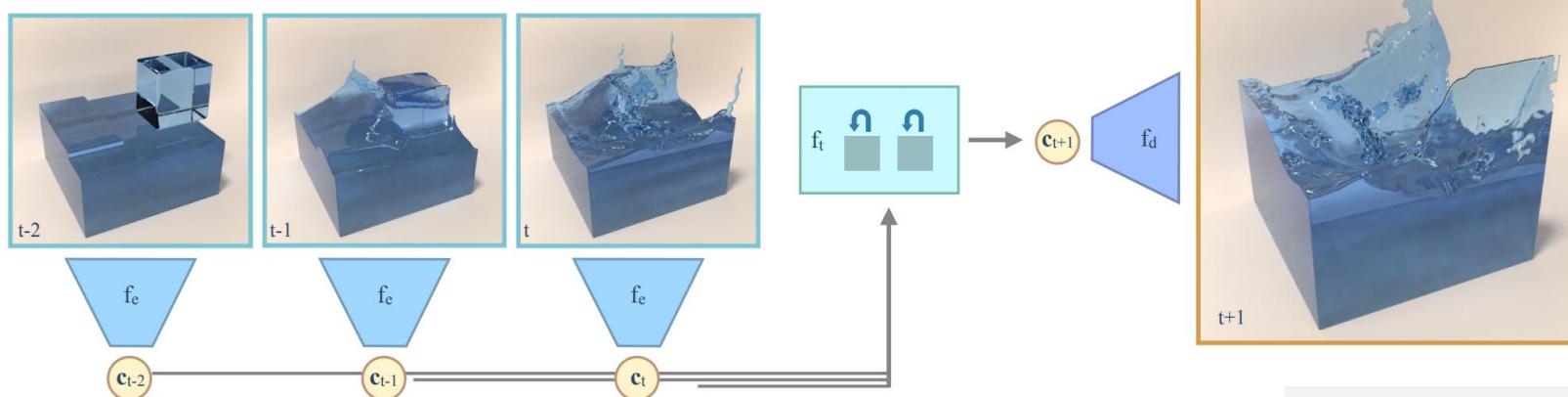
## » Speed-Up



Ladicky et al. 2015



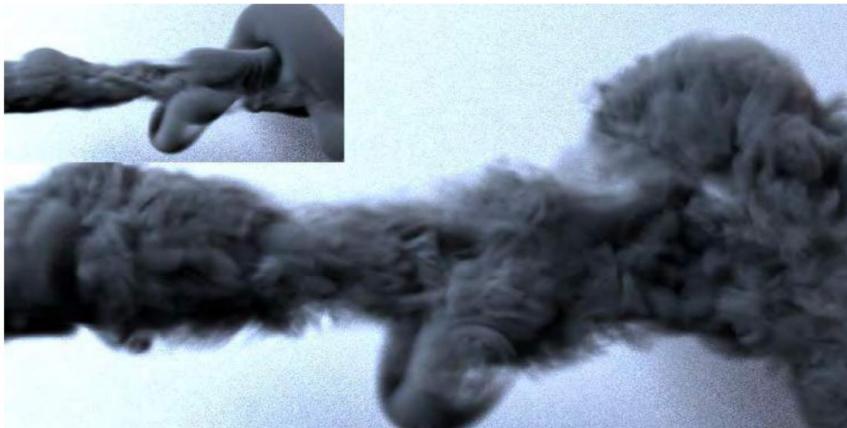
Tompson et al. 2016



Wiewel et al. 2019

# Machine Learning for Fluid Simulation

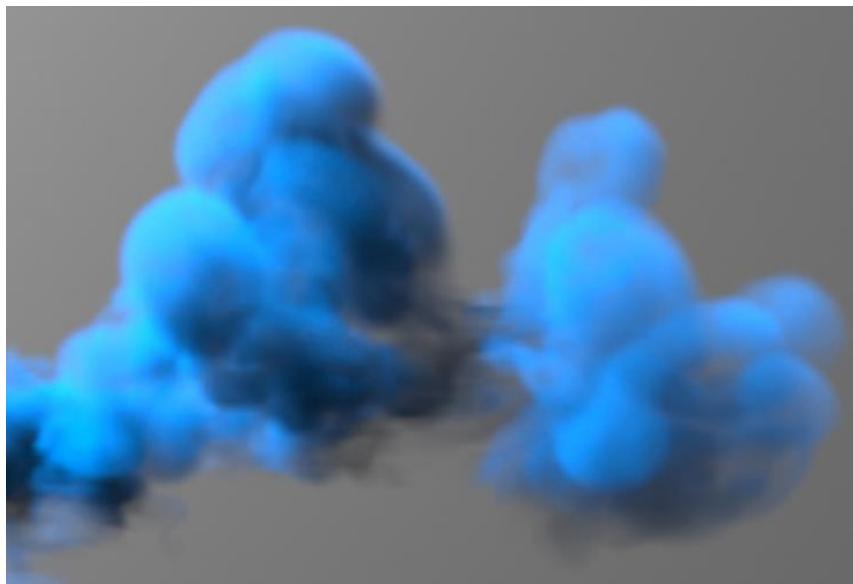
## » Enhance Visual Quality



Chu & Thuerey 2017

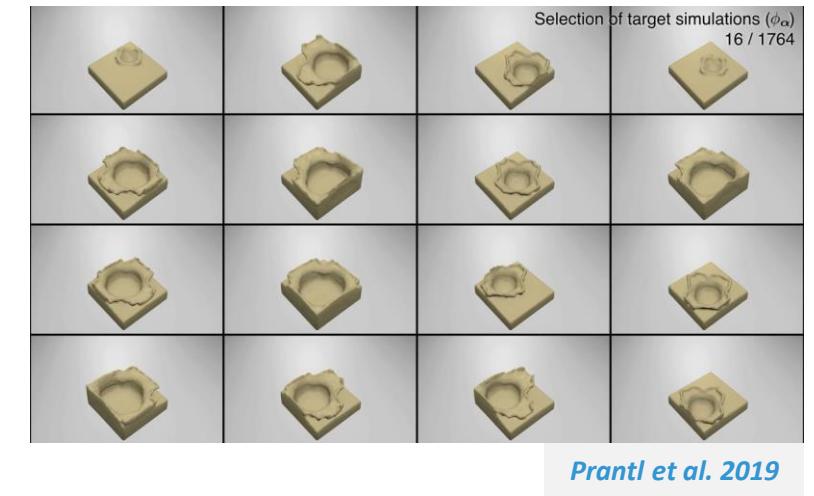
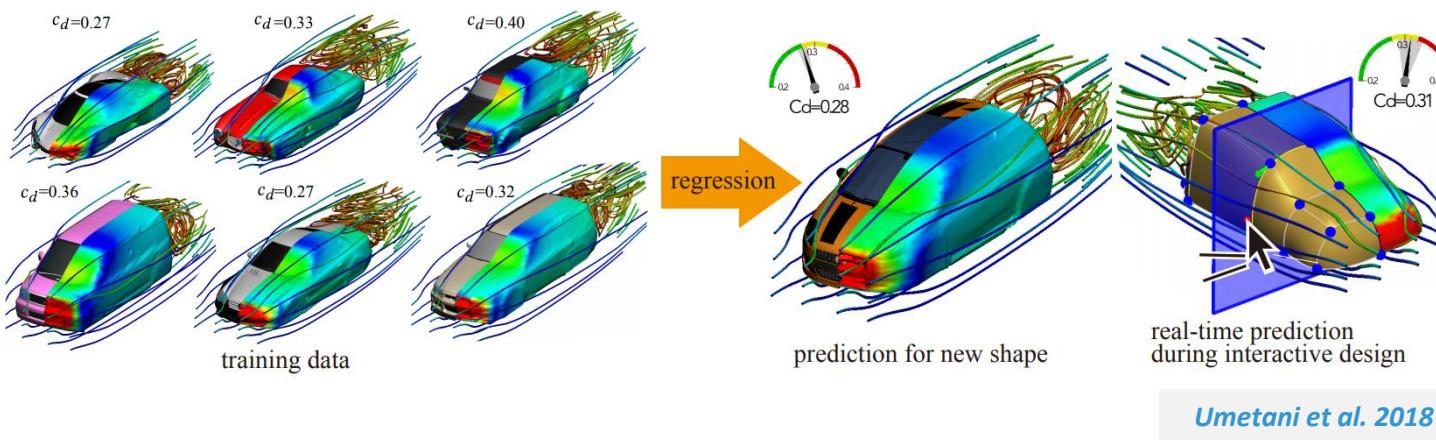


Um et al. 2018

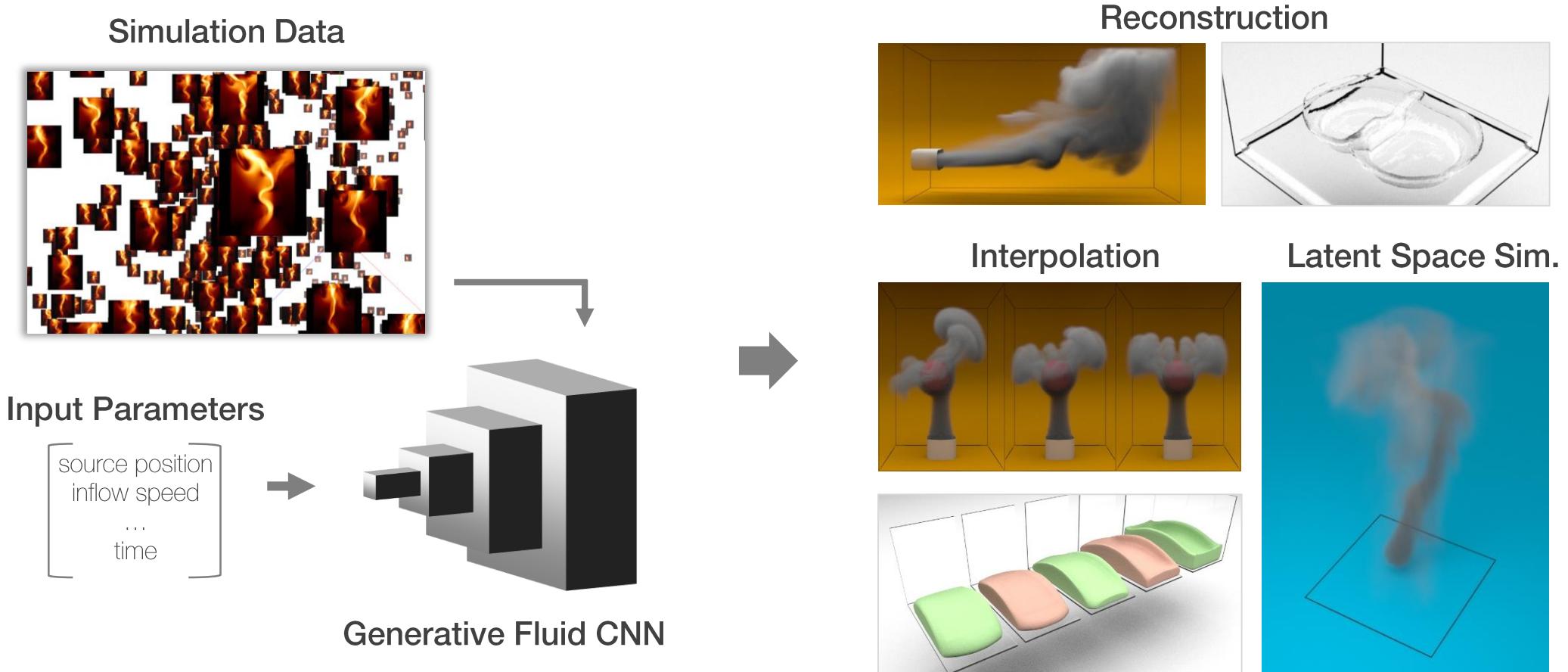


Xie et al. 2018

## » Generative Model



## » Generative Model



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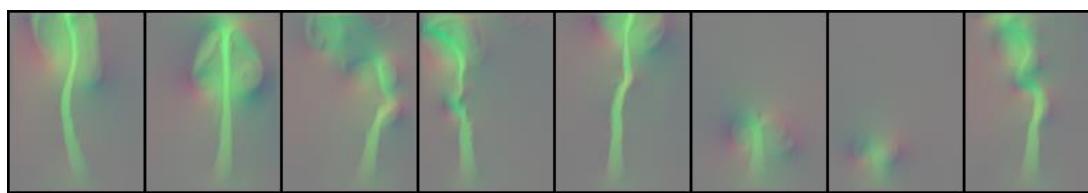
# A Generative Model for Fluids

# Fluid Simulation Data

## » vs. Image Dataset (CelebA)



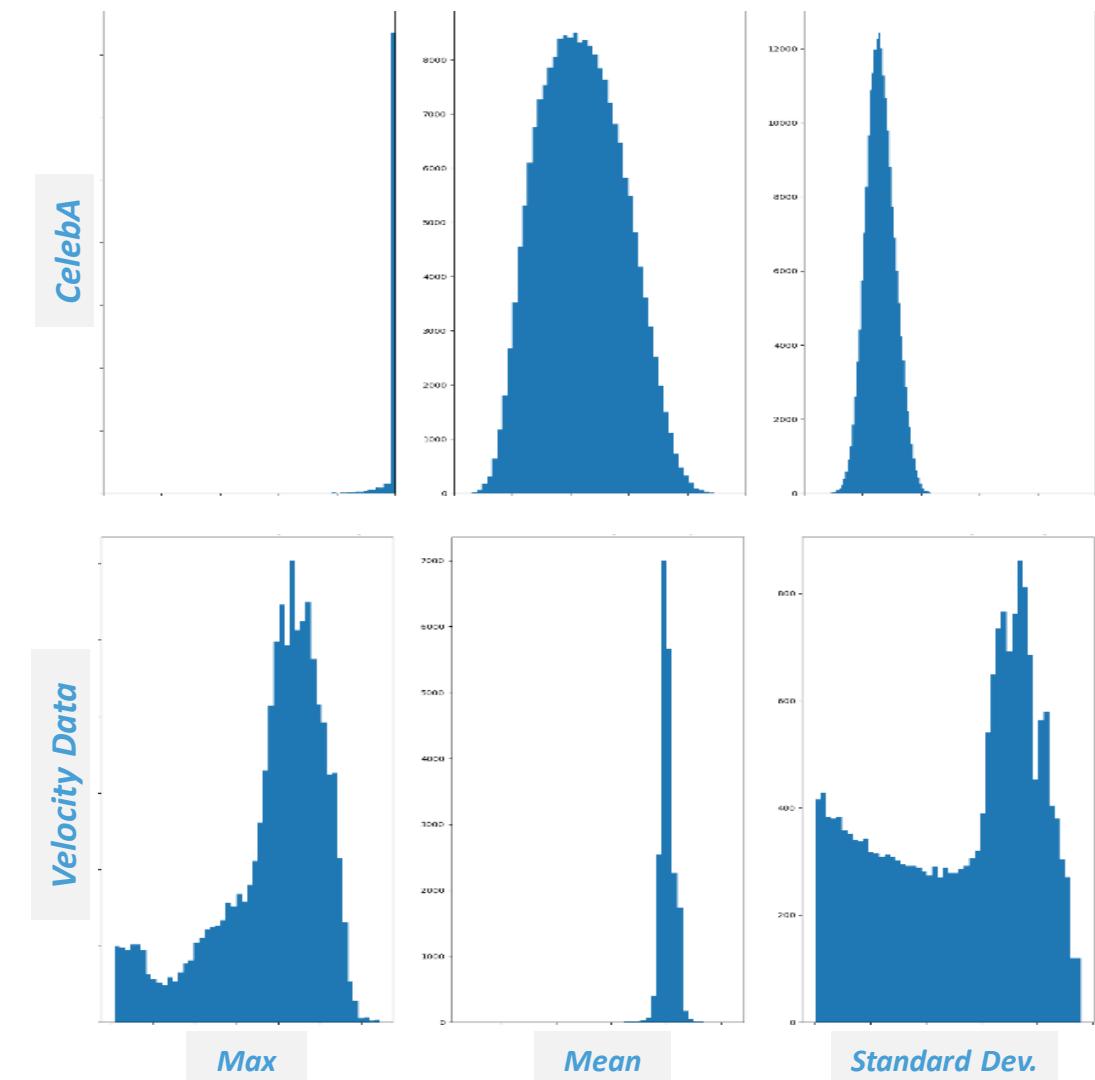
CelebA



Velocity Data

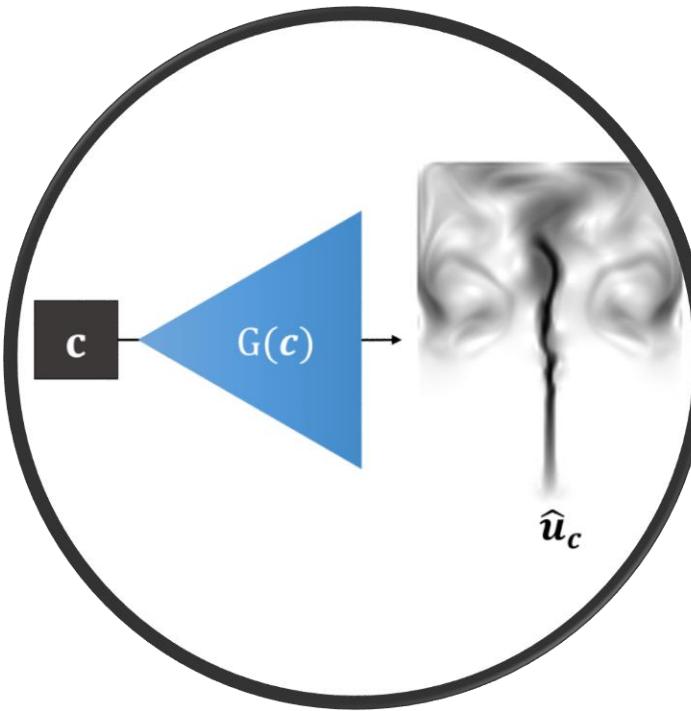
- Velocity fields differ from images
  - Spatial-temporal data which not possess “Eigenshapes”
  - Different statistical features
  - Standard image-based networks are not optimal

## Histogram plots

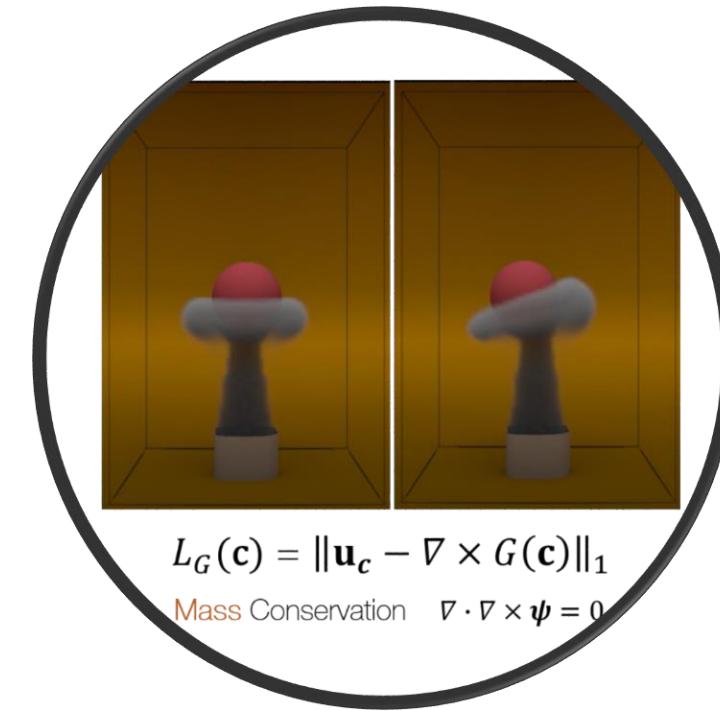




Dataset



Architecture



Loss Function

# Fluid Simulation Data

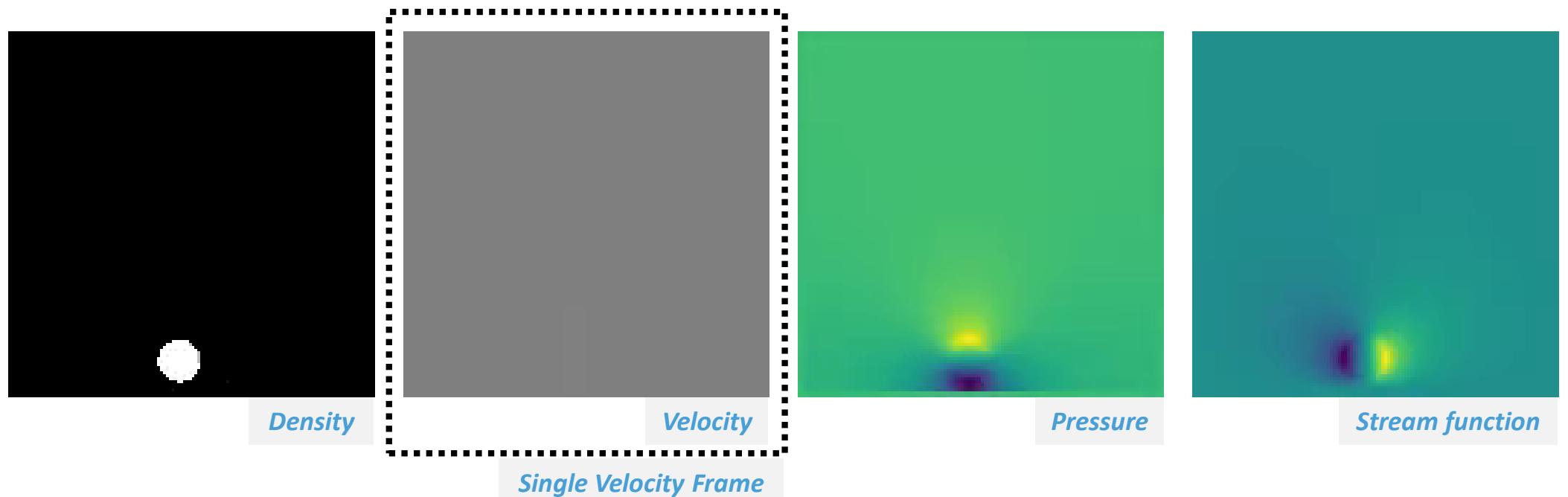
» Density, Velocity, Pressure and Stream function

$$\frac{\partial \mathbf{u}}{\partial t} = \mathbf{g} - \mathbf{u} \cdot \nabla \mathbf{u} - \frac{1}{\rho} \nabla p + \mu \nabla \cdot \nabla \mathbf{u}$$

Momentum Conservation

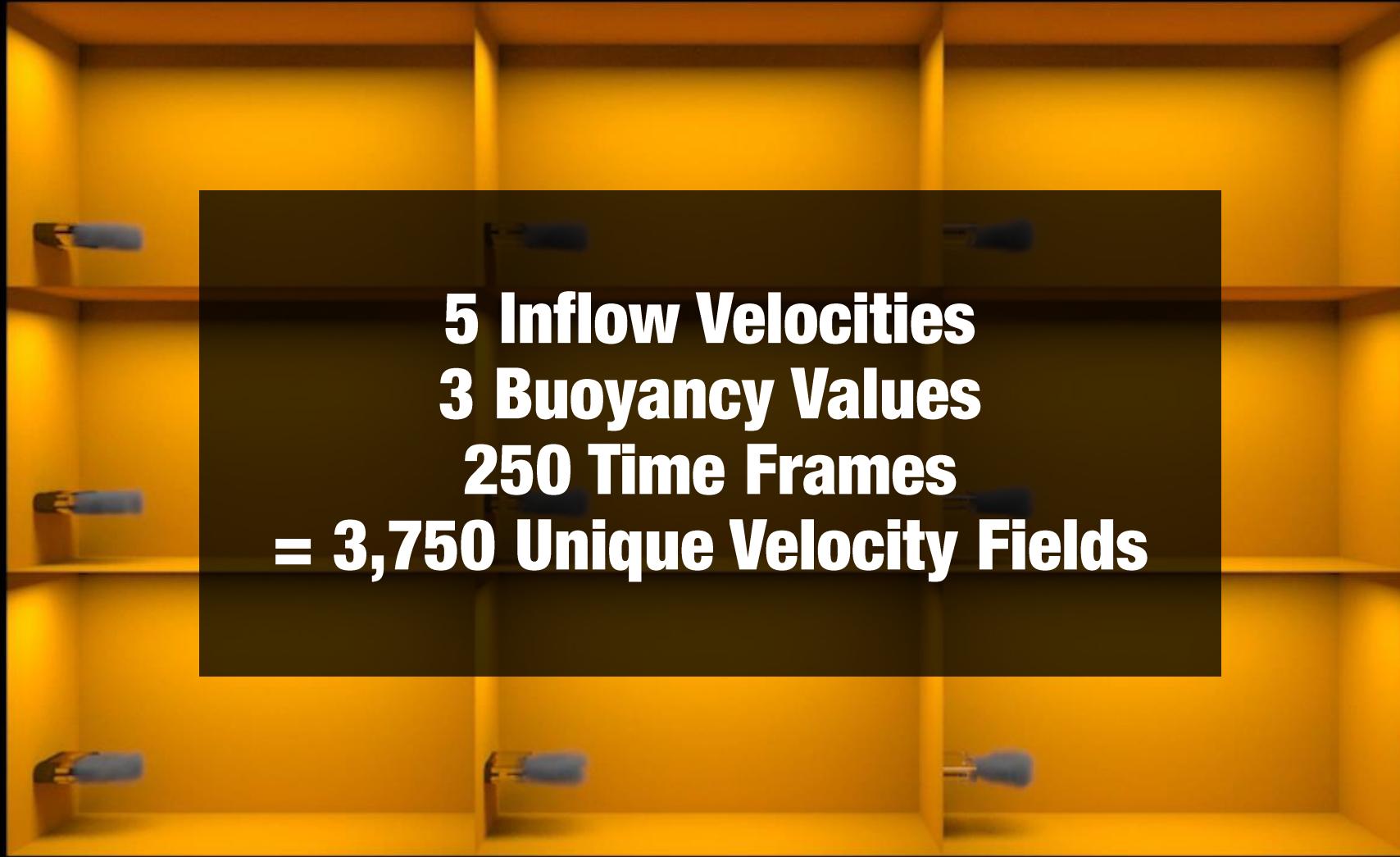
$$\nabla \cdot \mathbf{u} = 0$$

Mass Conservation



# Inflow Velocity

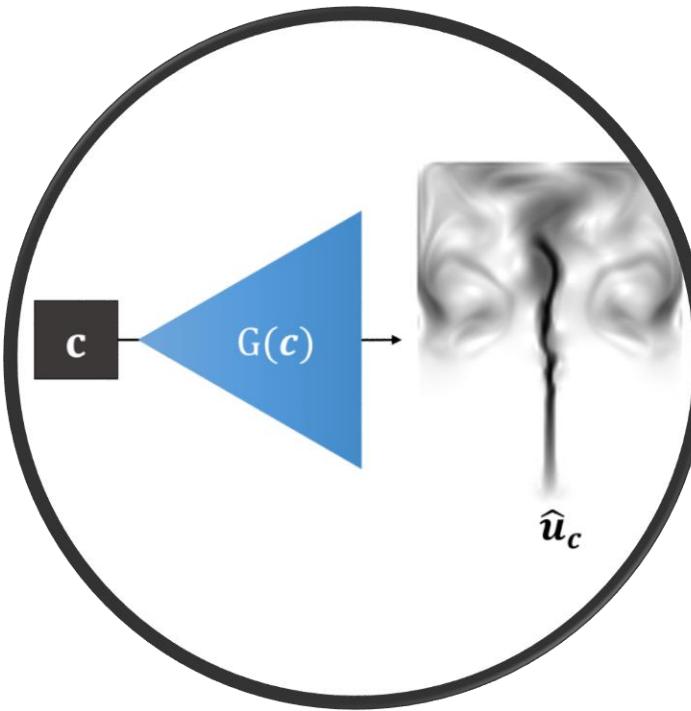
Buoyancy



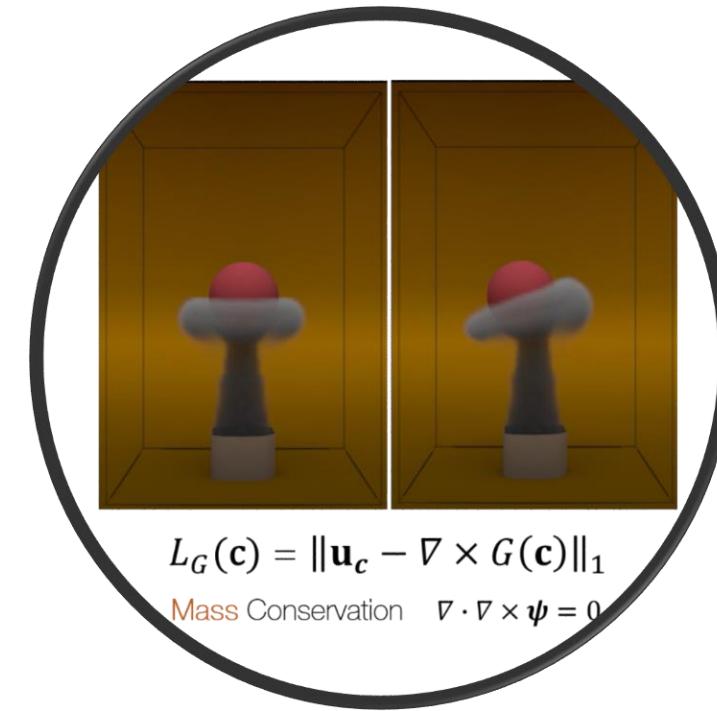
Ground-truth (simulated) velocity-field examples  
Input Parameters [velocity, buoyancy, time]



Dataset



Architecture

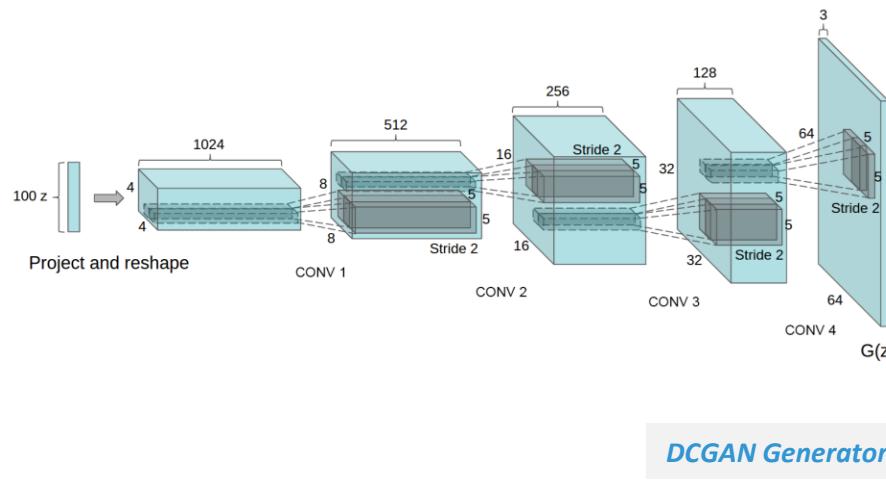


Loss Function

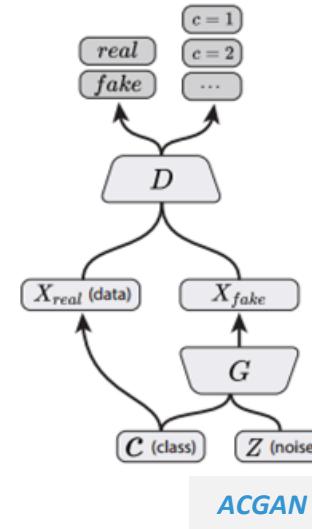
# Generative Model

## » Supervised vs. Unsupervised Learning

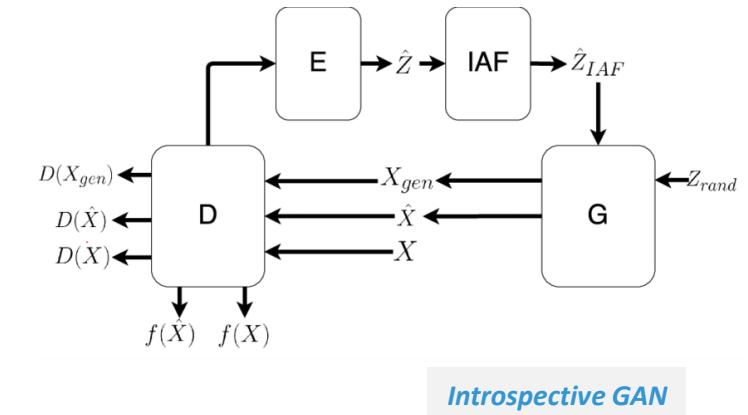
- Tried several unsupervised architectures



DCGAN Generator

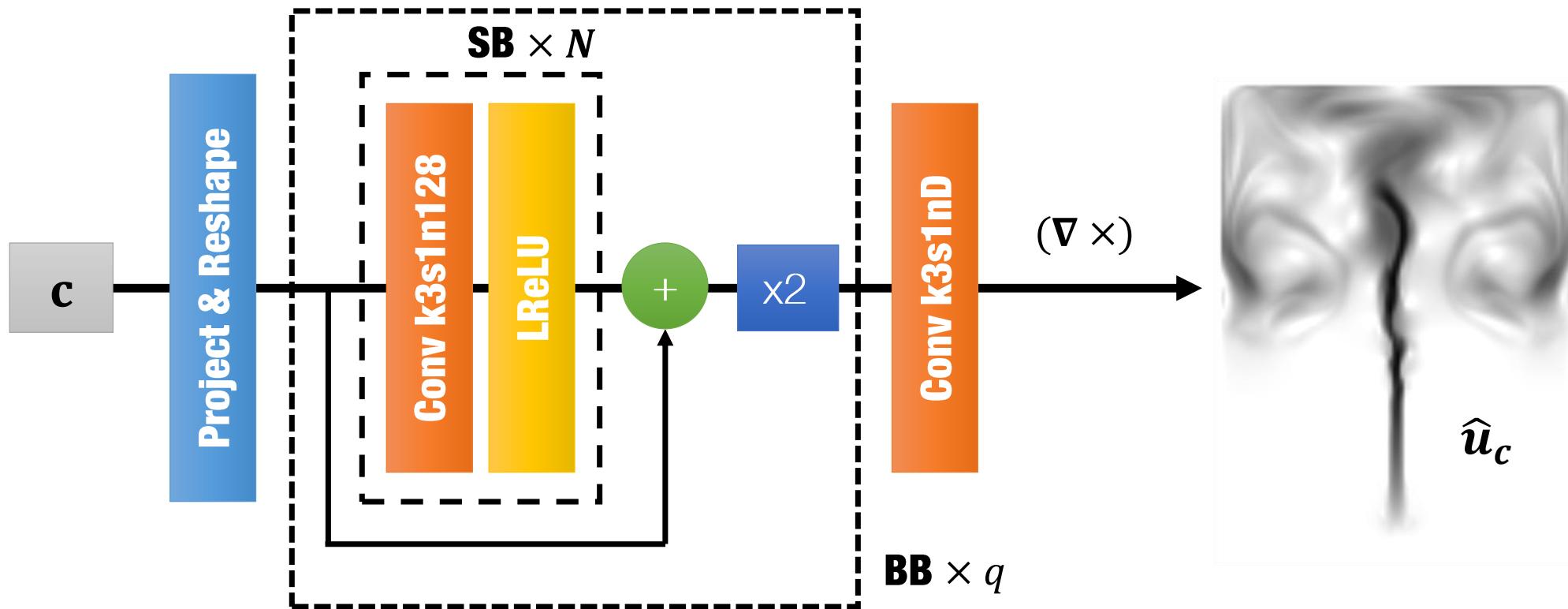


ACGAN



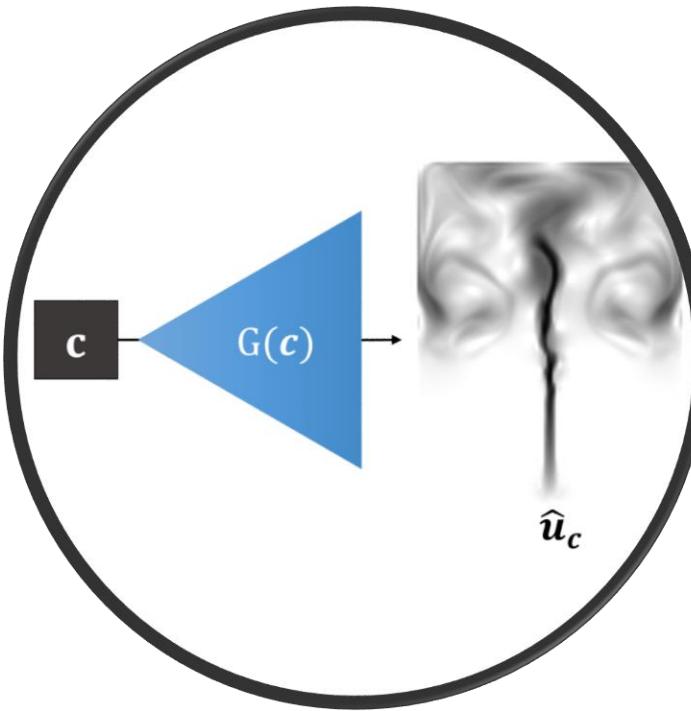
Introspective GAN

- Energy-Based GAN
- Least-Squares GAN
- Boundary Equilibrium GAN

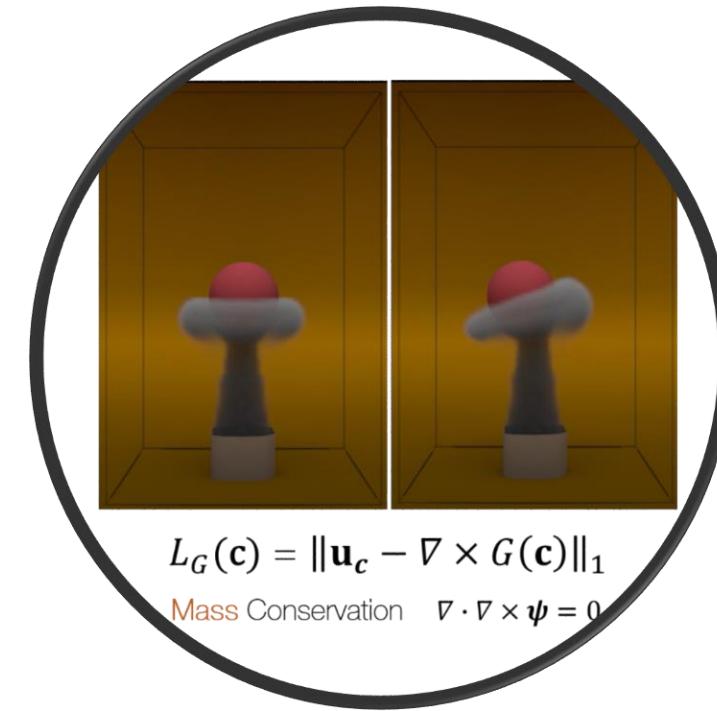




Dataset



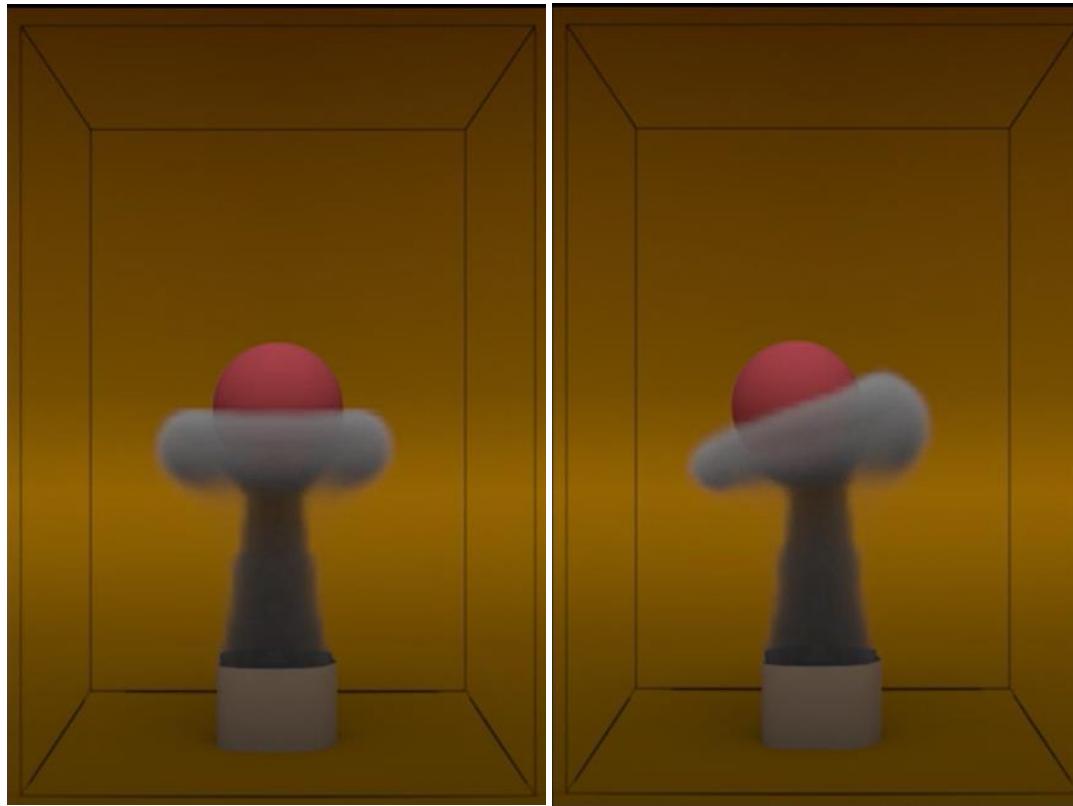
Architecture



Loss Function

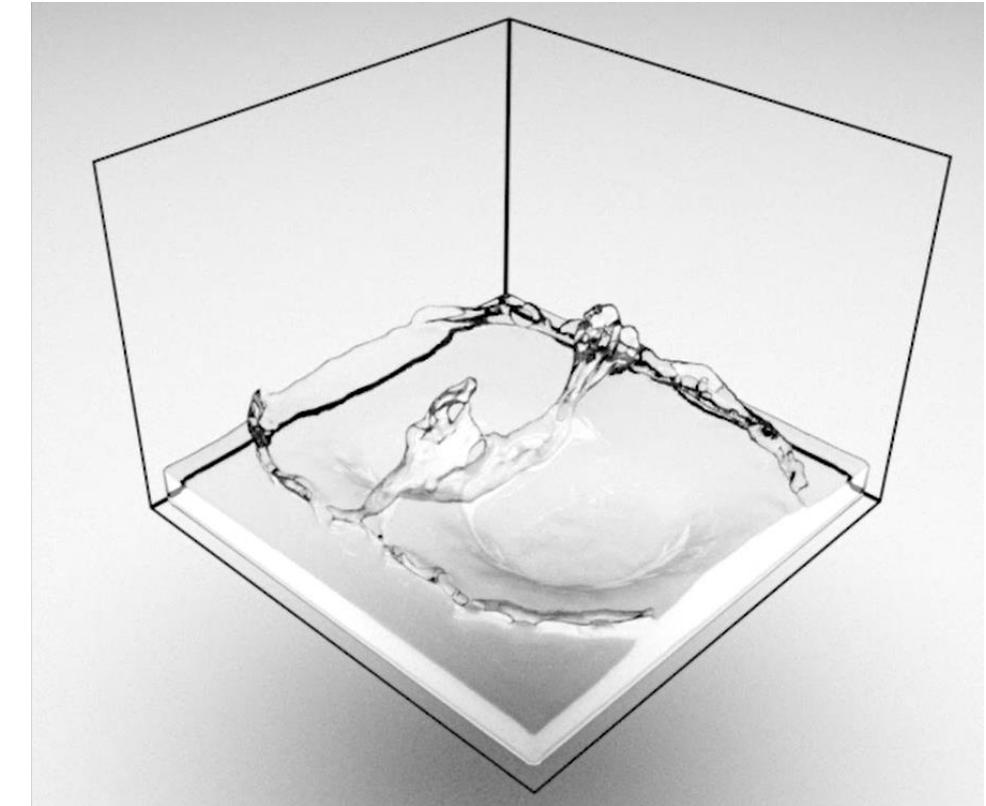
# Generative Model

## » Stream Function based Loss Function



$$L_G(\mathbf{c}) = \|\mathbf{u}_c - \nabla \times G(\mathbf{c})\|_1$$

Mass Conservation  $\nabla \cdot \nabla \times \psi = 0$

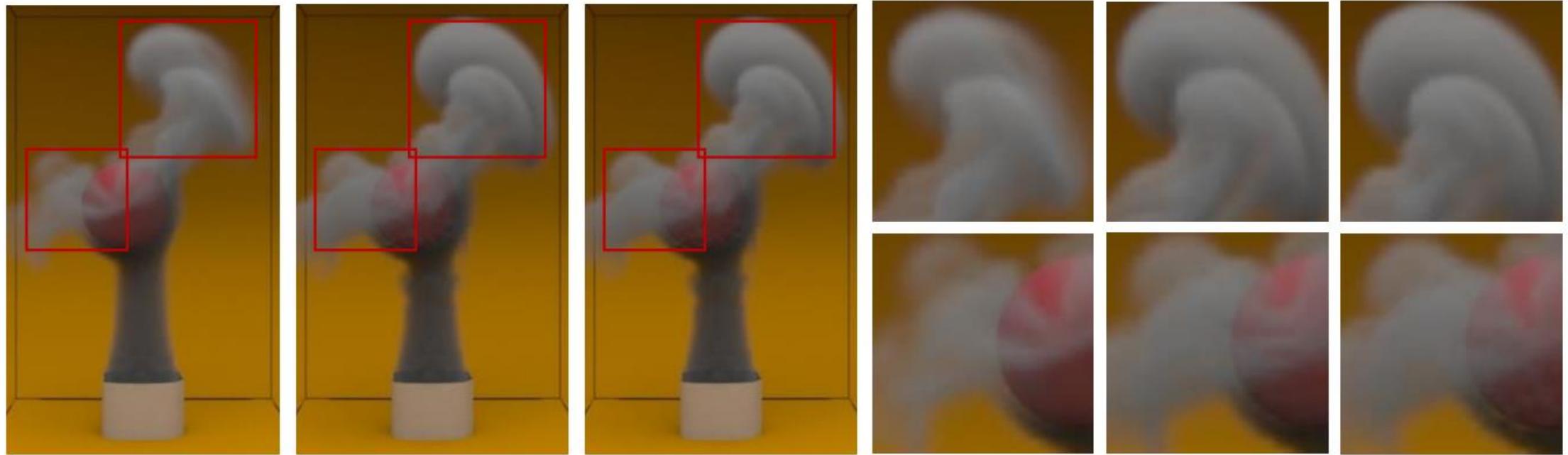


$$L_G(\mathbf{c}) = \|\mathbf{u}_c - G(\mathbf{c})\|_1$$

Partially Divergent Motion (Liquids)

# Generative Model

## » Comparison of Stream Function and Velocity based Loss Functions



$$\hat{\mathbf{u}}_{\mathbf{c}} = G(\mathbf{c})$$

$$\hat{\mathbf{u}}_{\mathbf{c}} = \nabla \times G(\mathbf{c})$$

G.t.

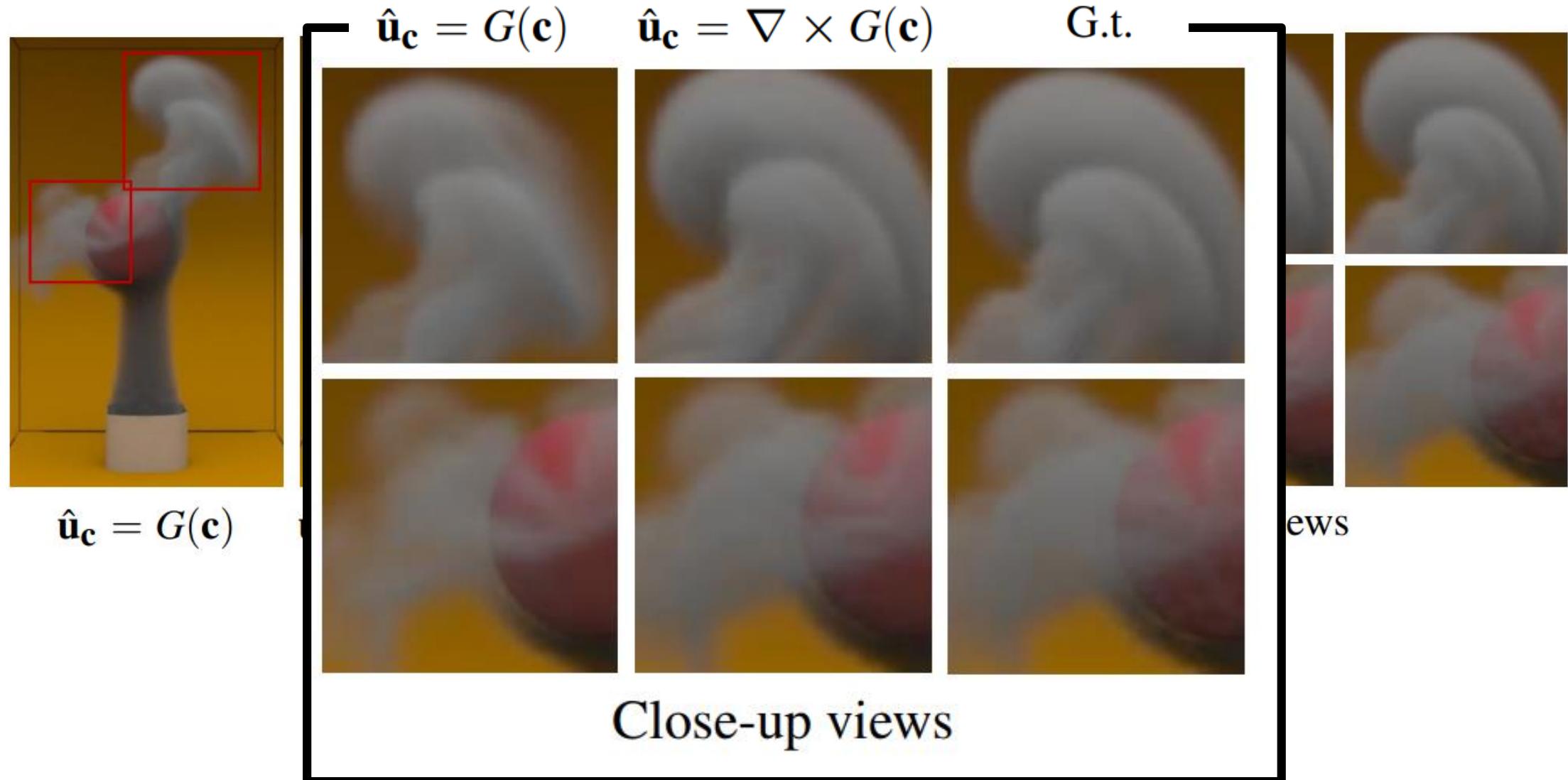
Close-up views

$$L_G(\mathbf{c}) = \|\mathbf{u}_c - \nabla \times G(\mathbf{c})\|_1$$

Mass Conservation  $\nabla \cdot \nabla \times \psi = 0$

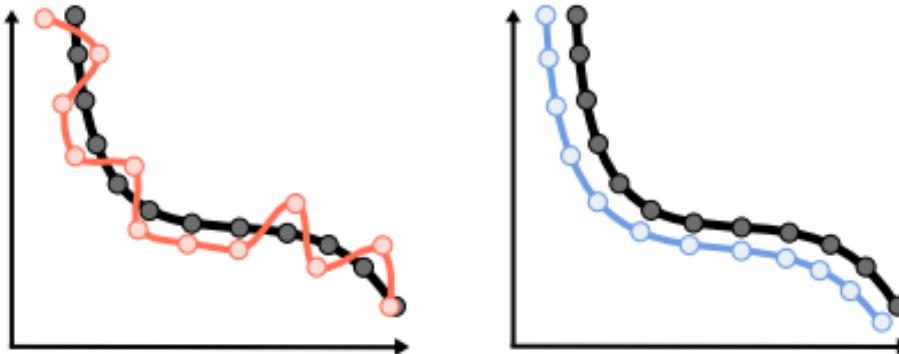
# Generative Model

## » Comparison of Stream Function and Velocity based Loss Functions



# Generative Model

## » Jacobian Loss Function for Smooth Data

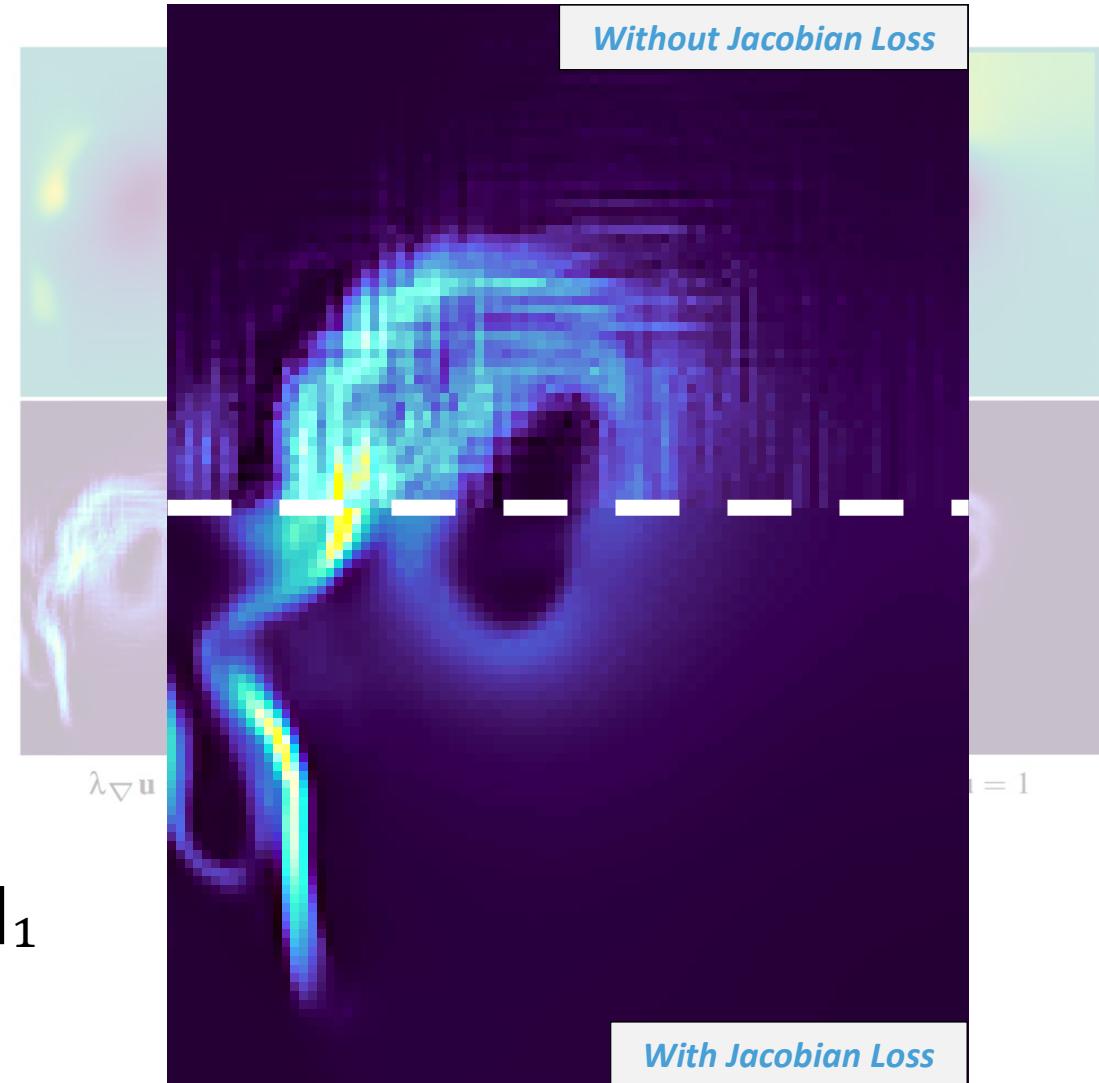


*Same L1 Loss Function Value*

- Pure L1 loss function does not pin-down derivatives for smooth data
- We increment the loss to also match derivatives of the original data

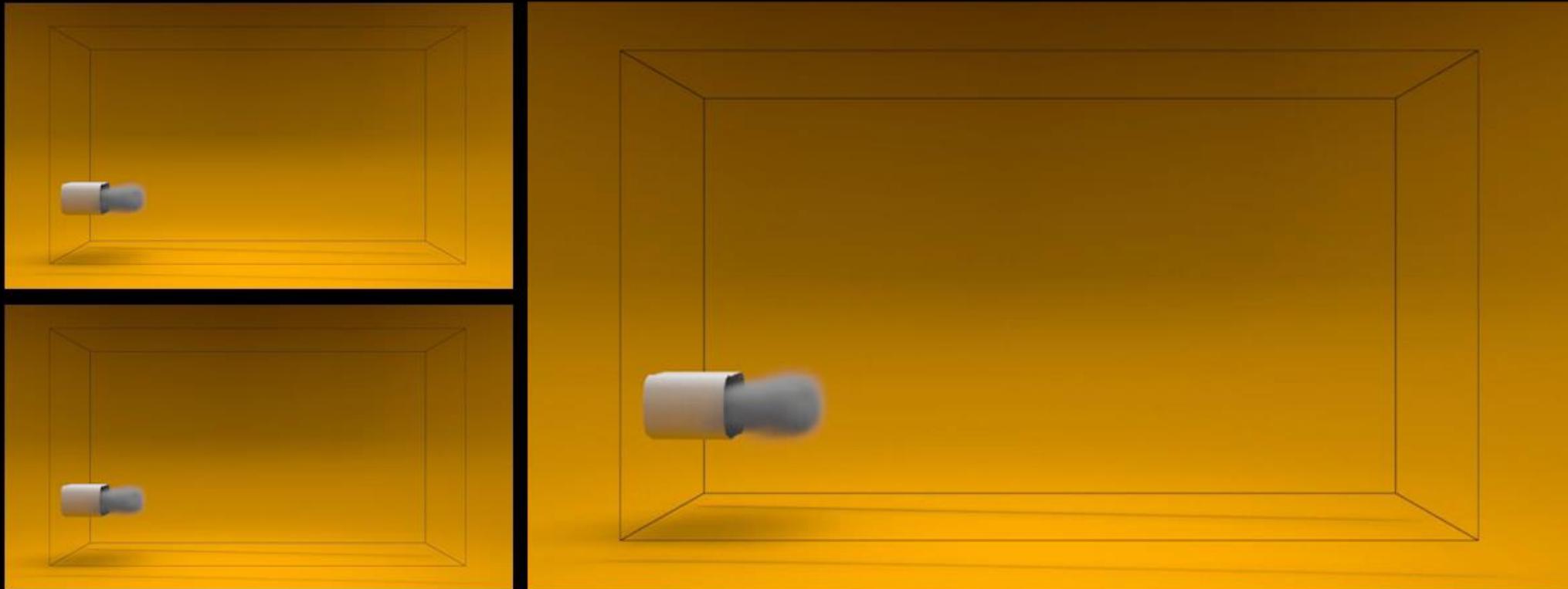
$$L_G(\mathbf{c}) = \lambda_{\mathbf{u}} \|\mathbf{u}_c - \hat{\mathbf{u}}_c\|_1 + \lambda_{\nabla \mathbf{u}} \|\nabla \mathbf{u}_c - \nabla \hat{\mathbf{u}}_c\|_1$$

where  $\hat{\mathbf{u}}_c = \nabla \times G(\mathbf{c})$  or  $\hat{\mathbf{u}}_c = G(c)$



# Results for Parameterizable Scenes

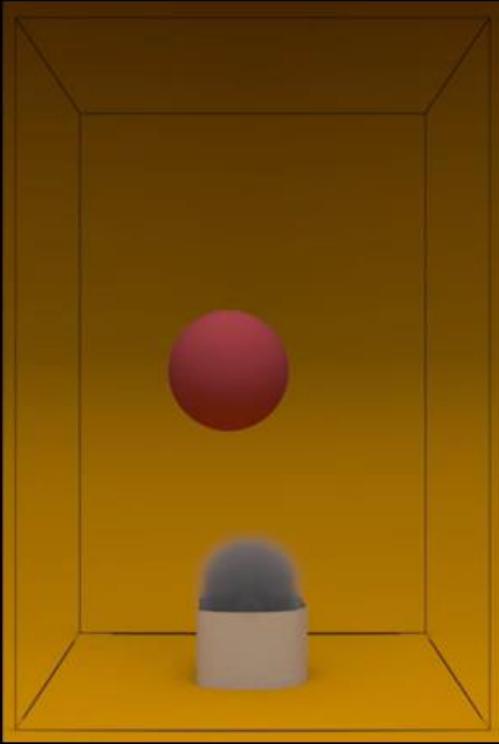
## Inflow Velocity Interpolation Example



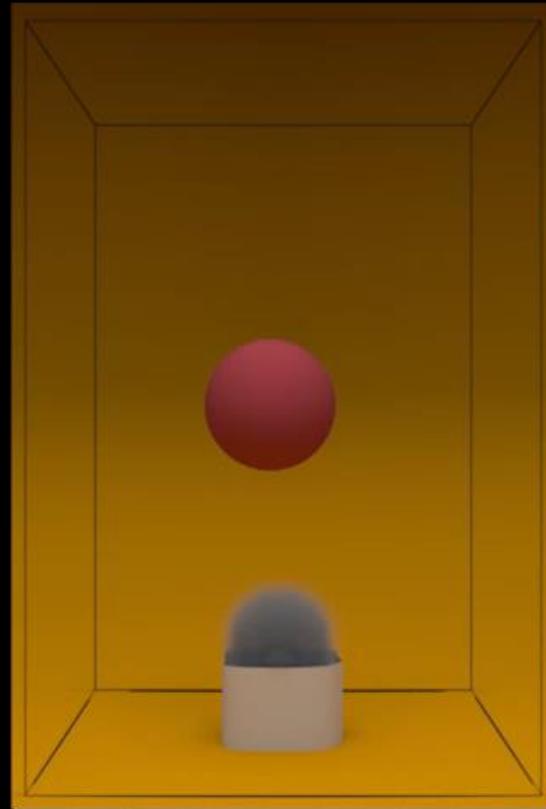
**Direct** correspondence  
for velocities  $v_x = 4$  and  $v_x = 5$

**Interpolated** with  $v_x = 4.5$ , **Not present** in the original **data set**

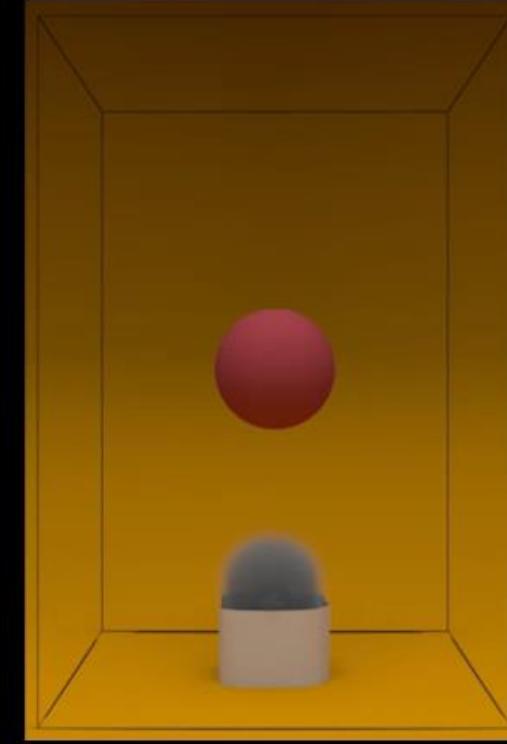
## Obstacle Scene Interpolation



**CNN Reconstruction**  
for position  $p_x = 0.44$

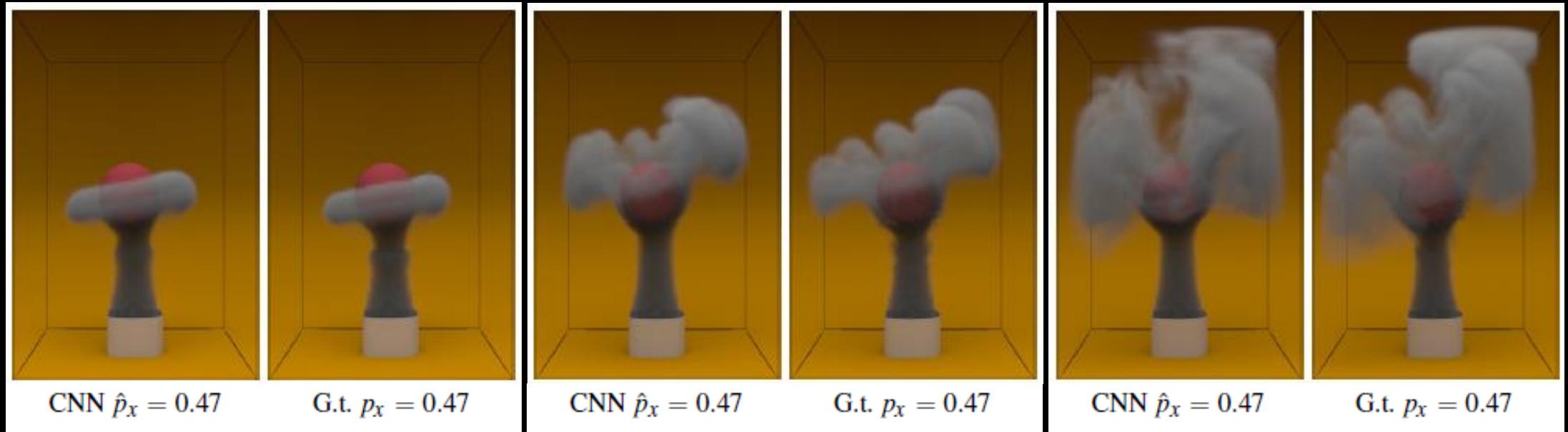


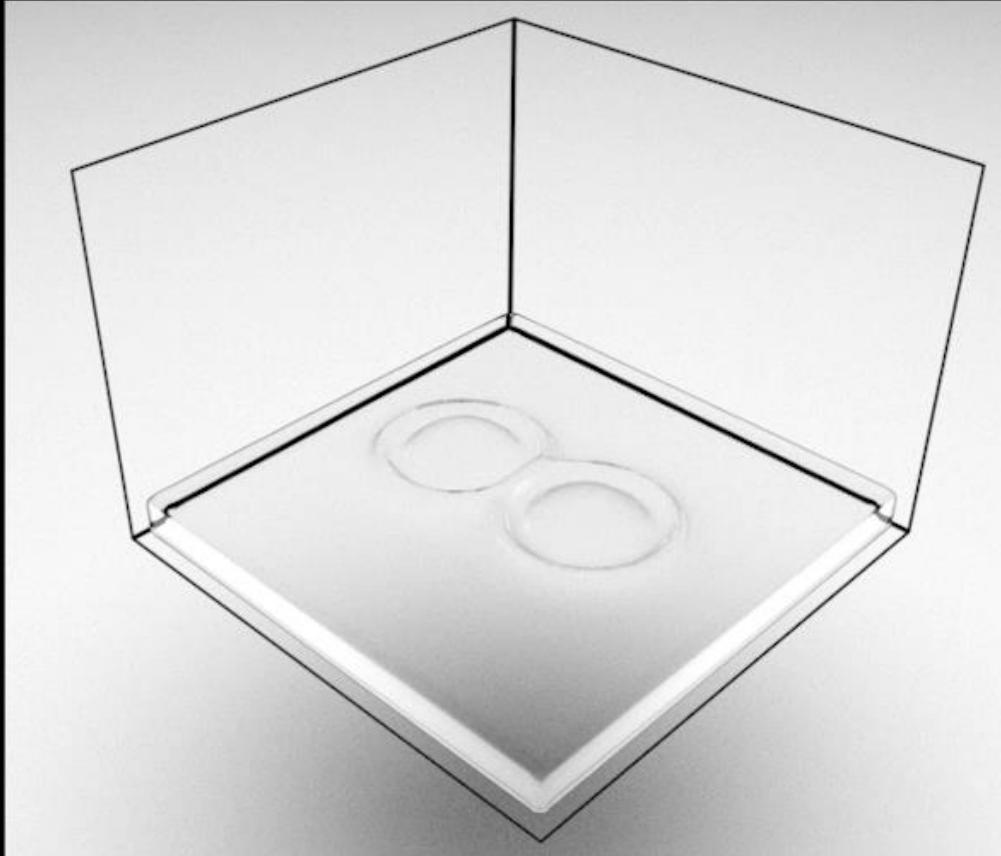
**CNN Interpolation** for  
position  $p_x = 0.47$



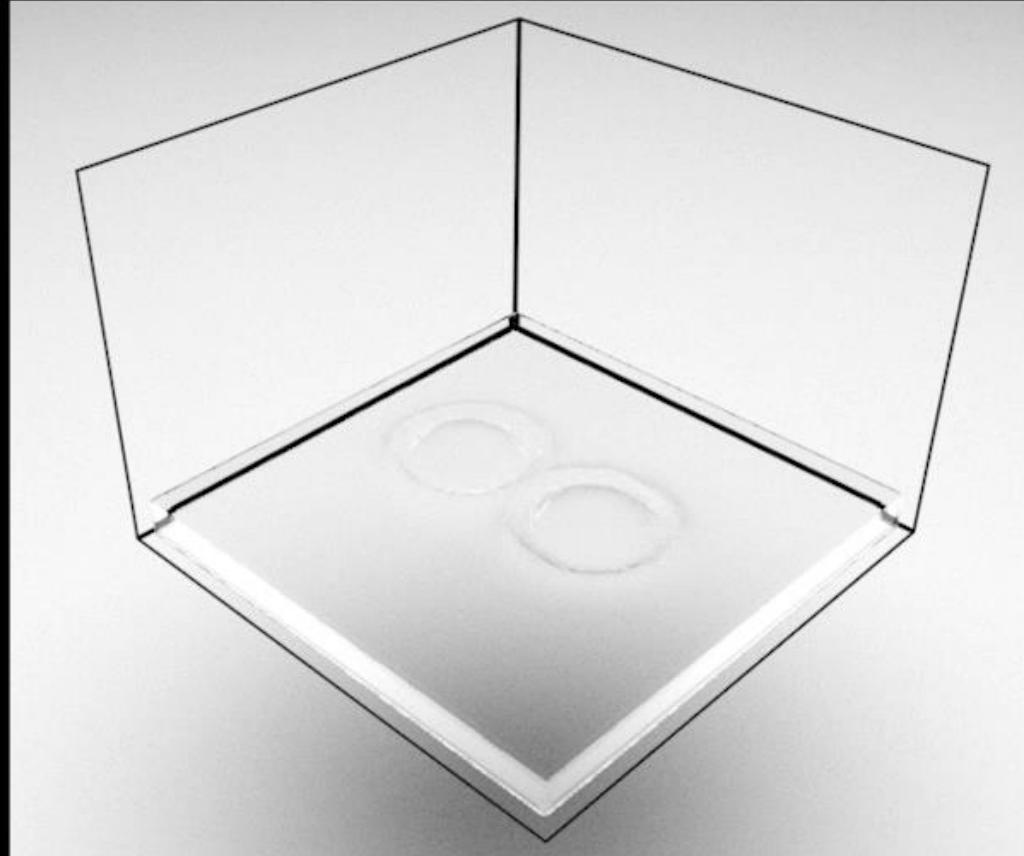
**CNN Reconstruction**  
for position  $p_x = 0.50$

# Deep Fluids: Obstacle Scene

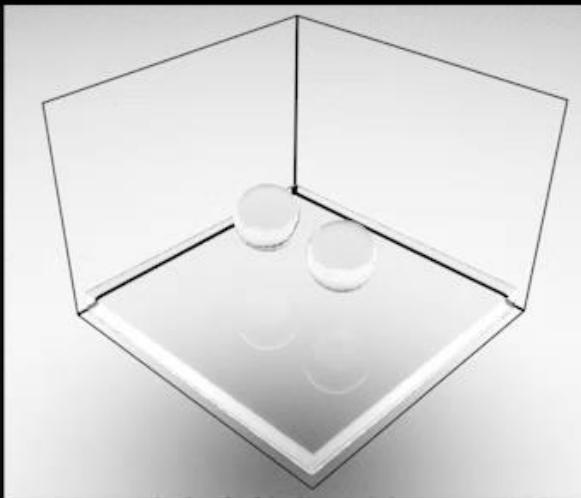




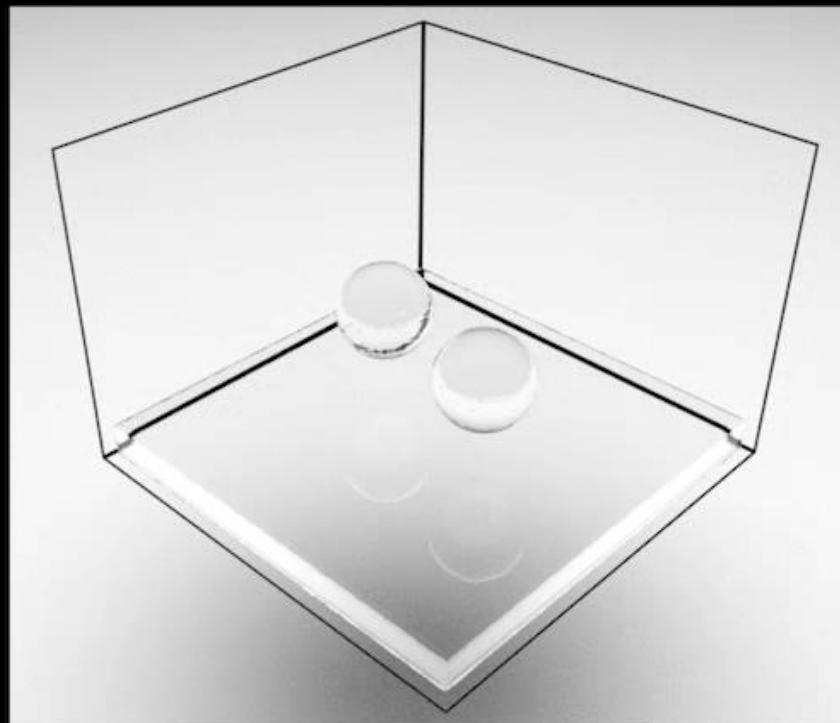
**Ground-Truth**



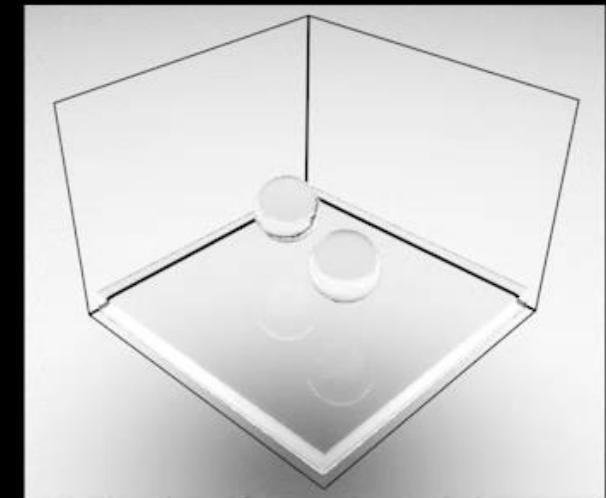
**Reconstructed** by our **CNN**



**CNN Reconstruction** for  
distance  $d = 0.15$  and  
angle  $\theta = 0^\circ$



**CNN Interpolation** for  
distance  $d = 0.1625$  and  
angle  $\theta = 9^\circ$



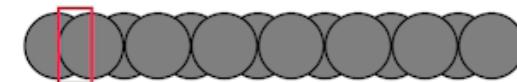
**CNN Reconstruction** for  
distance  $d = 0.175$  and  
angle  $\theta = 18^\circ$



**10 Positions**

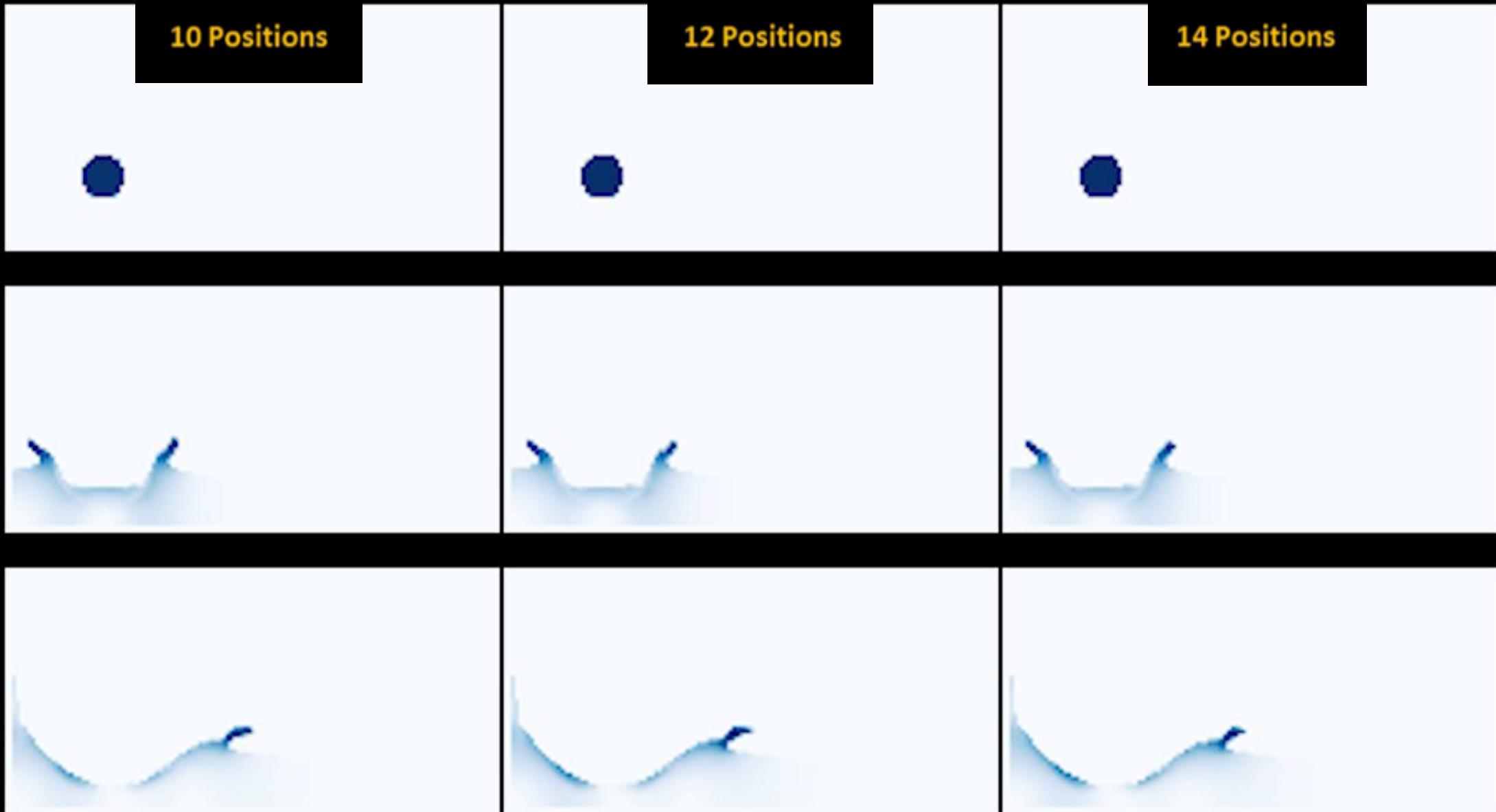


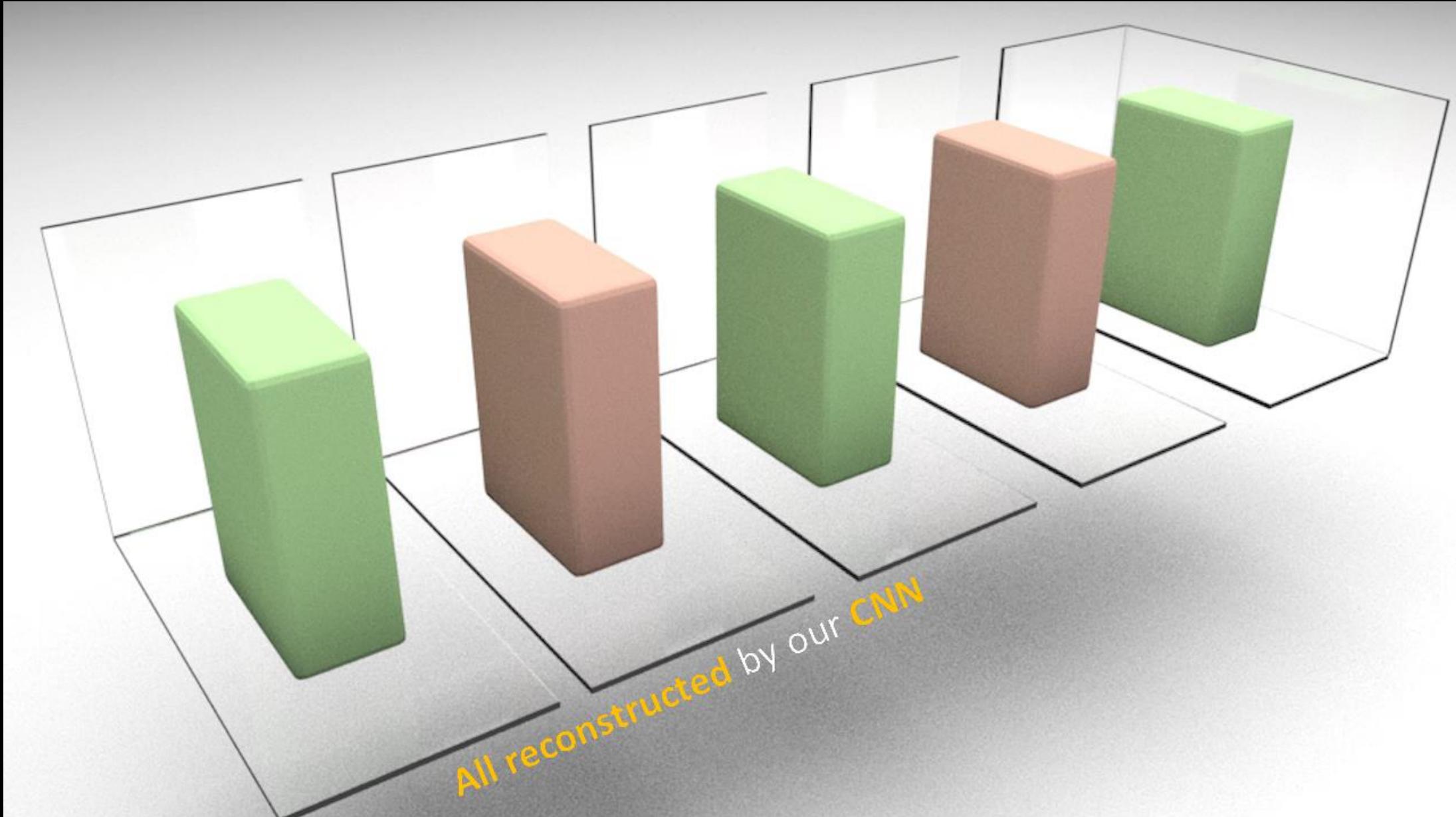
**12 Positions**

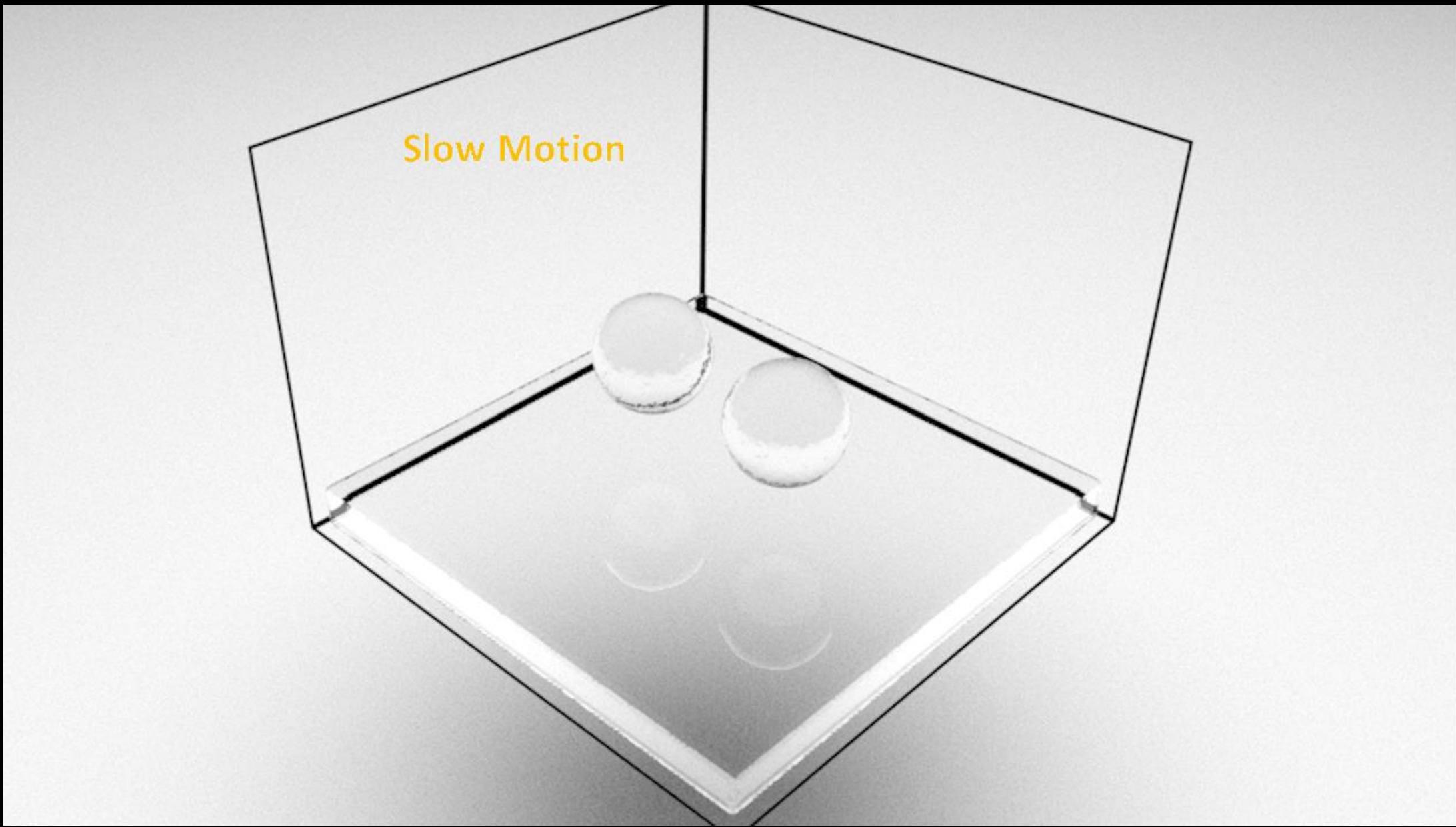


**14 Positions**

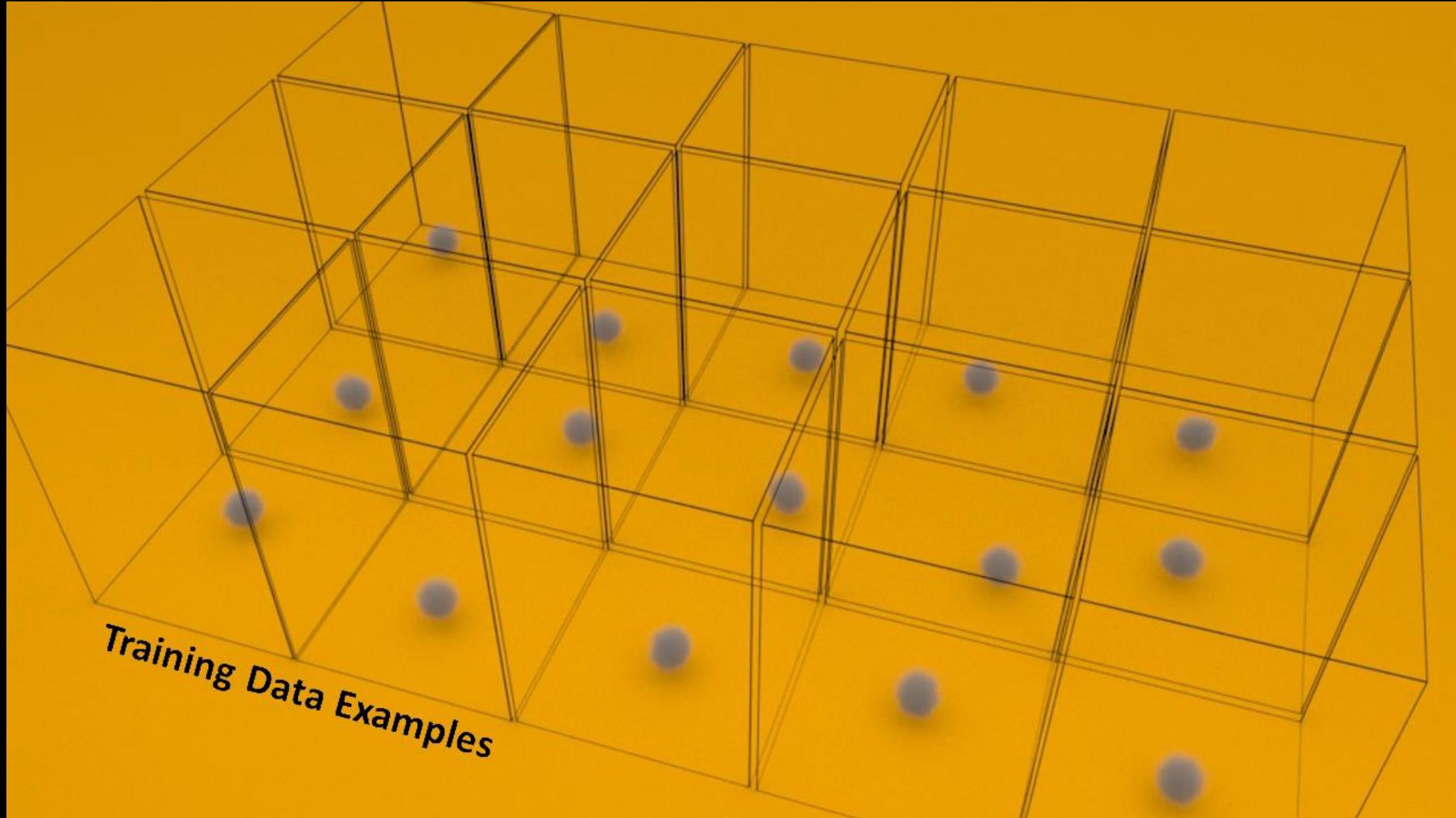
# Deep Fluids: Liquids in 2D







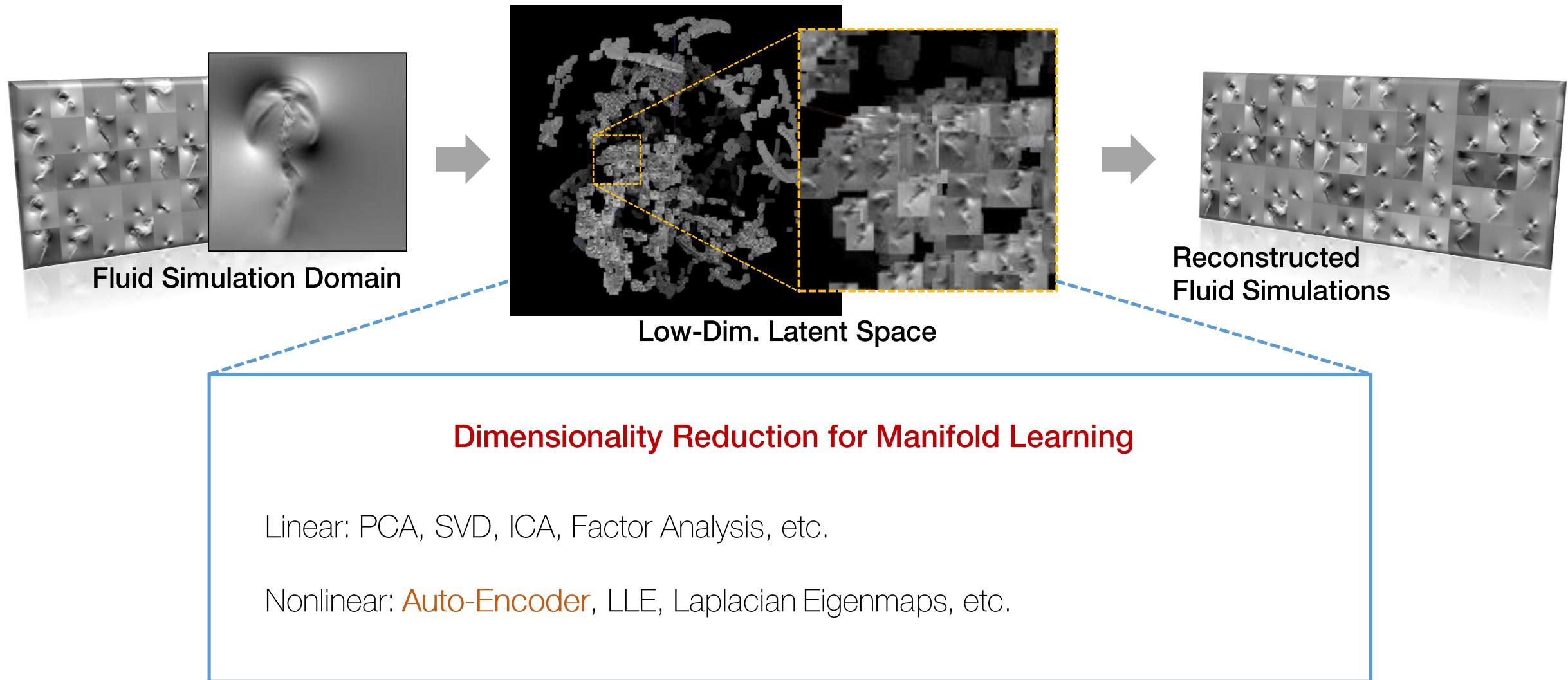
# Towards Extended Parameterizations



Input Parameters [history of source positions, time]

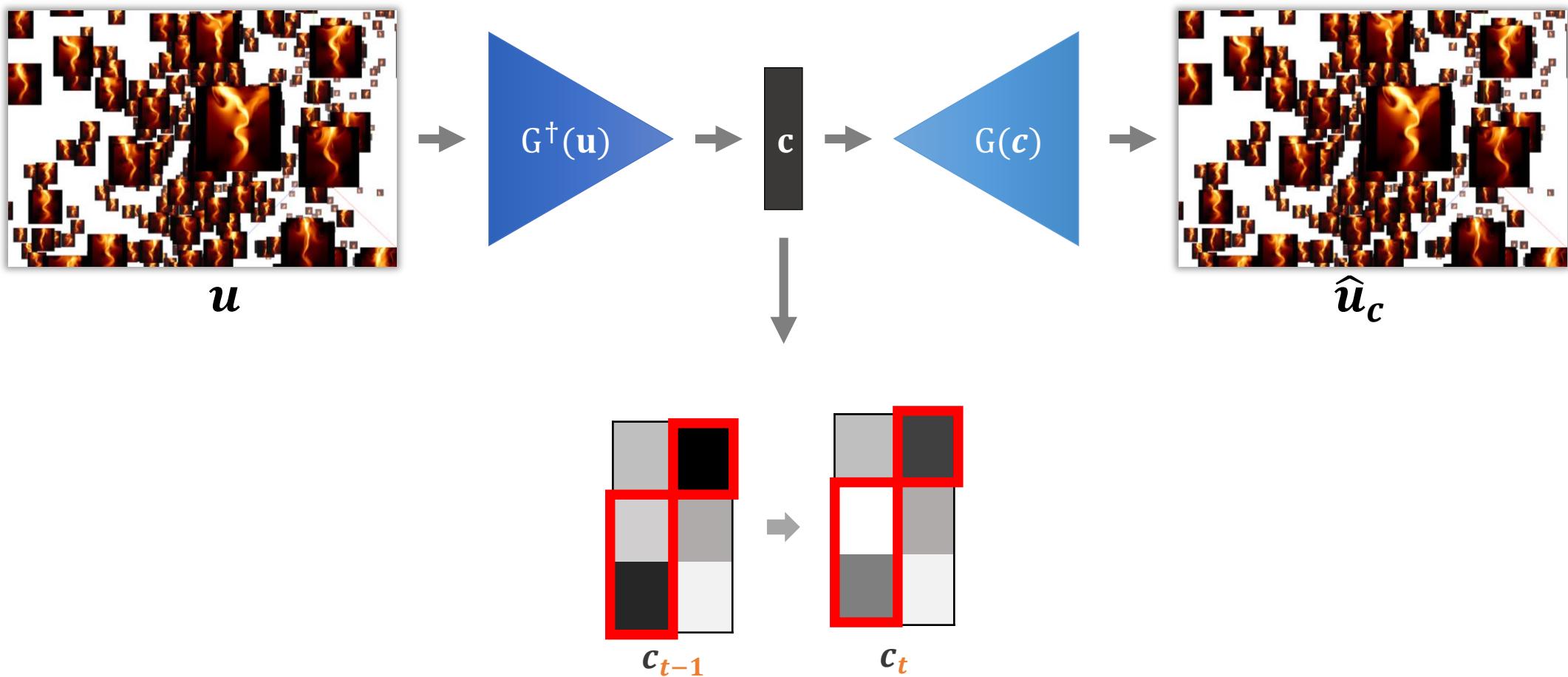
# Extended Parameterizations

## » Learning a Fluid Data Manifold



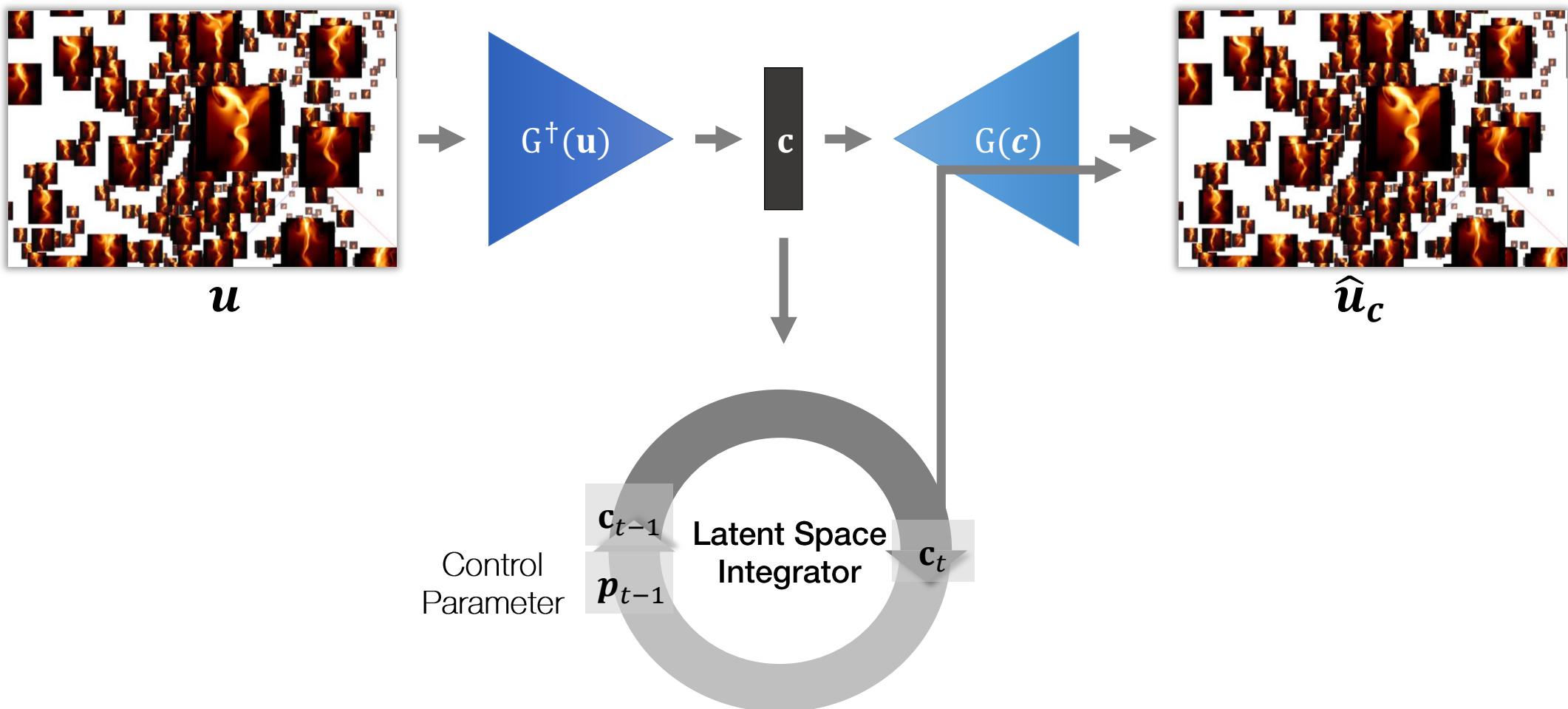
# Extended Parameterizations

## » Latent-Space Integration

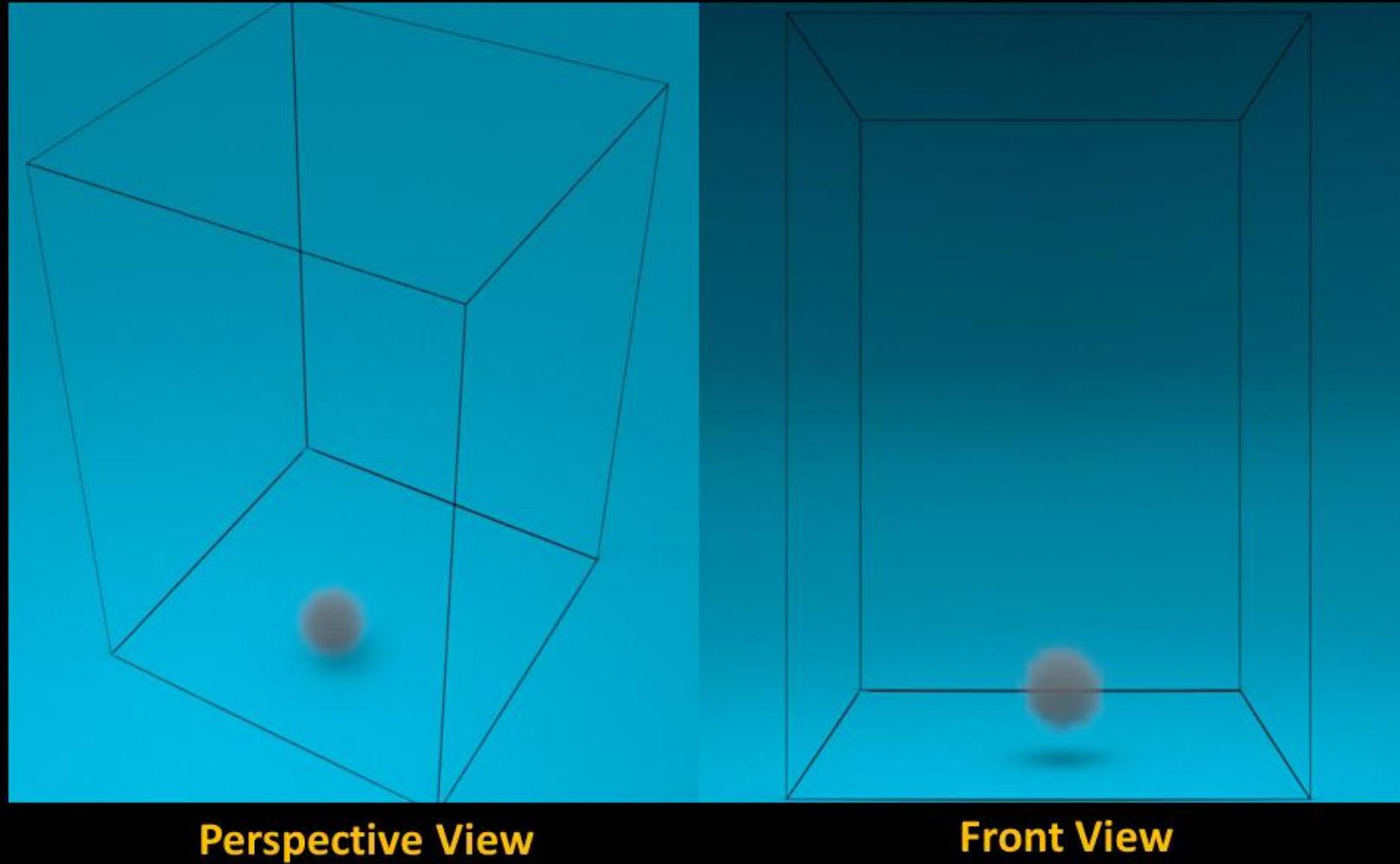


# Extended Parameterizations

## » Latent-Space Integration



## Latent Space Simulation: New Source Motion

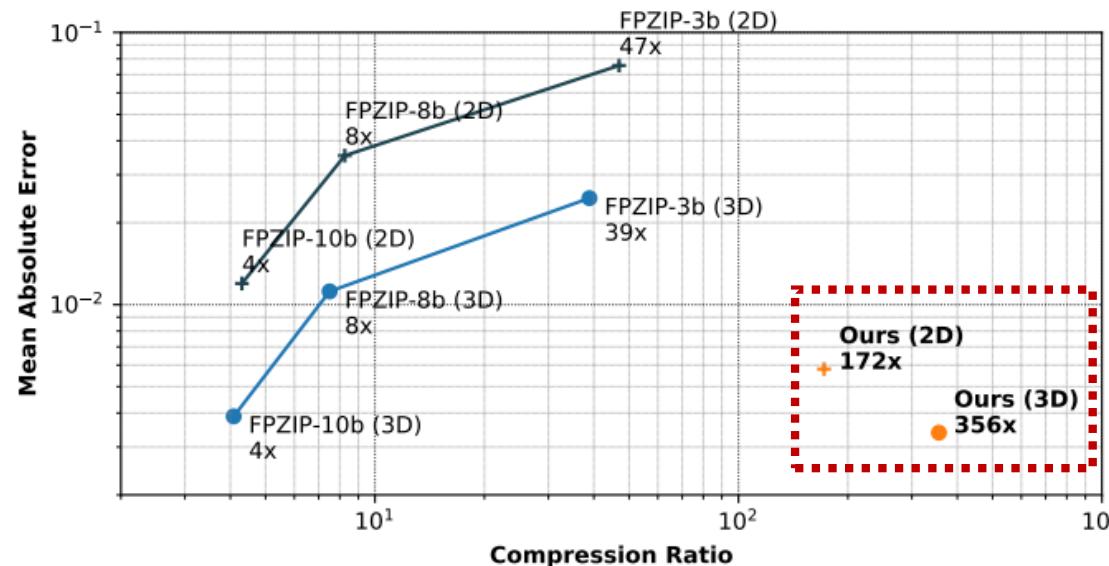


Perspective View

Front View

# Performance

| Scene          | Grid<br>Resolution        | # Frames | Simulation<br>Time (s) | Eval. Time<br>(ms) [Batch] | Speed Up<br>( $\times$ ) | Data Set<br>Size (MB) | Network<br>Size (MB) | Compression<br>Ratio | Training<br>Time (h) |
|----------------|---------------------------|----------|------------------------|----------------------------|--------------------------|-----------------------|----------------------|----------------------|----------------------|
| Smoke Plume    | $96 \times 128$           | 21,000   | 0.033                  | 0.052 [100]                | 635                      | 2064                  | 12                   | 172                  | 5                    |
| Smoke Obstacle | $64 \times 96 \times 64$  | 6,600    | 0.491                  | 0.999 [5]                  | 513                      | 31143                 | 30                   | 1038                 | 74                   |
| Smoke Inflow   | $112 \times 64 \times 32$ | 3,750    | 0.128                  | 0.958 [5]                  | 128                      | 10322                 | 29                   | 356                  | 40                   |
| Liquid Drops   | $96 \times 48 \times 96$  | 7,500    | 0.172                  | 1.372 [3]                  | 125                      | 39813                 | 30                   | 1327                 | 134                  |
| Viscous Dam    | $96 \times 72 \times 48$  | 600      | 0.984                  | 1.374 [3]                  | 716                      | 2389                  | 29                   | 82                   | 100                  |
| Rotating Smoke | $48 \times 72 \times 48$  | 500      | 0.08                   | 0.52 [10]                  | 308                      | 995                   | 38                   | 26                   | 49                   |
| Moving Smoke   | $48 \times 72 \times 48$  | 80,000   | 0.08                   | 0.52 [10]                  | 308                      | 159252                | 38                   | 4191*                | 49                   |



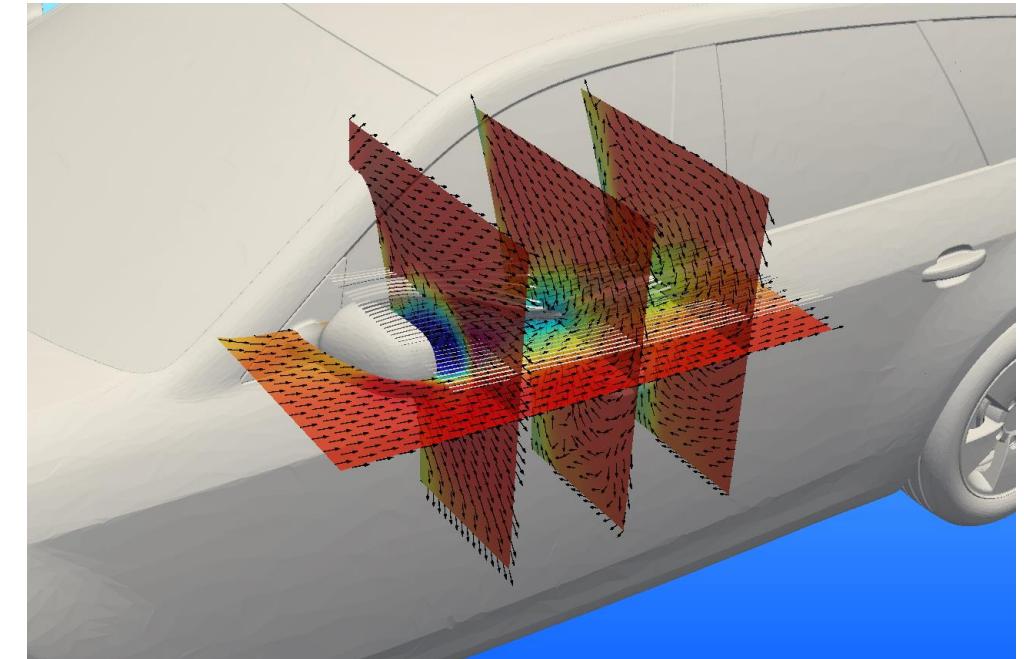
- **Quality of Reconstruction**
  - Reconstructed data is too smooth
    - GANs are useful for hallucinating high-frequency details but not physically plausible
  - Ghosting may happen if data is not sampled with enough density
  - Boundary Conditions introduce discontinuities that might leave liquid particles hanging
- **Latent Space Integration**
  - Learned latent space of AE can be improved
  - Using simply MLP for time integration is not optimal

## ■ Contributions

- Fast and plausible approximation of parameterized Eulerian fluid simulations with high compression ratio
- Novel latent space integrator
- Suitable for games and real-time virtual environments

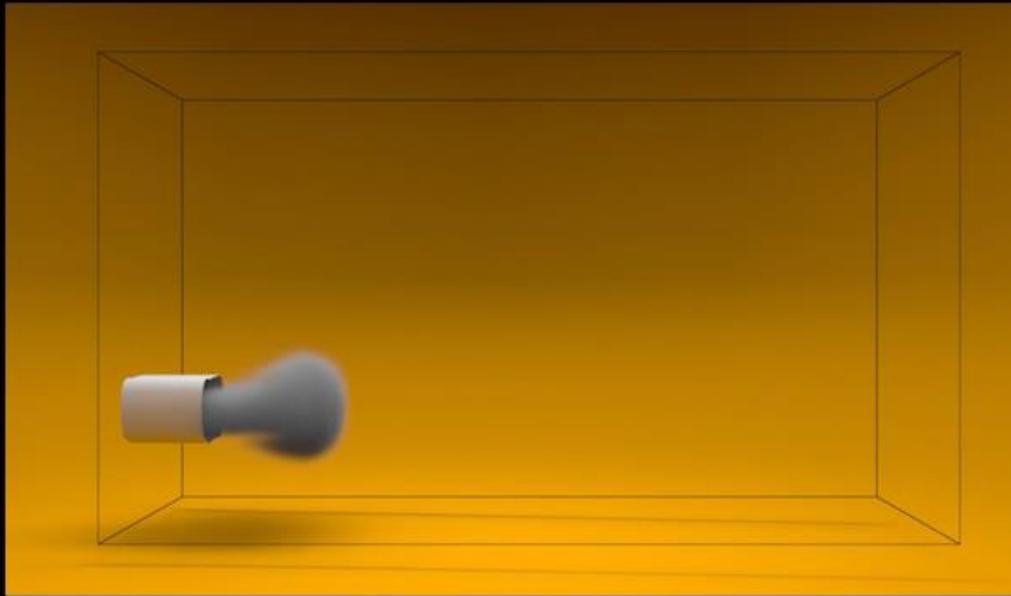
## ■ Future Work

- Boundary conditions
- Improved Latent-space integration LSTMs
- Bypassing modelling by directly reconstructing captured data



@Streamwise

Thanks for your attention [<https://github.com/byungsook/deep-fluids>]



**Ground-Truth** Simulation



**CNN-Reconstructed** Simulation